



AN OVERVIEW ABOUT THE BRAZILIAN ELECTRICITY MARKET: OPTIMIZATION AND PRICING

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Guest Lecture in Power Markets – Nicholas School of Environment

Duke
UNIVERSITY

Overview

- Introduction
- The Brazilian Electric Power System
- Coordination and Optimization of Resources
- Pricing Formation in the Electricity Market
- Final Comments

Introduction

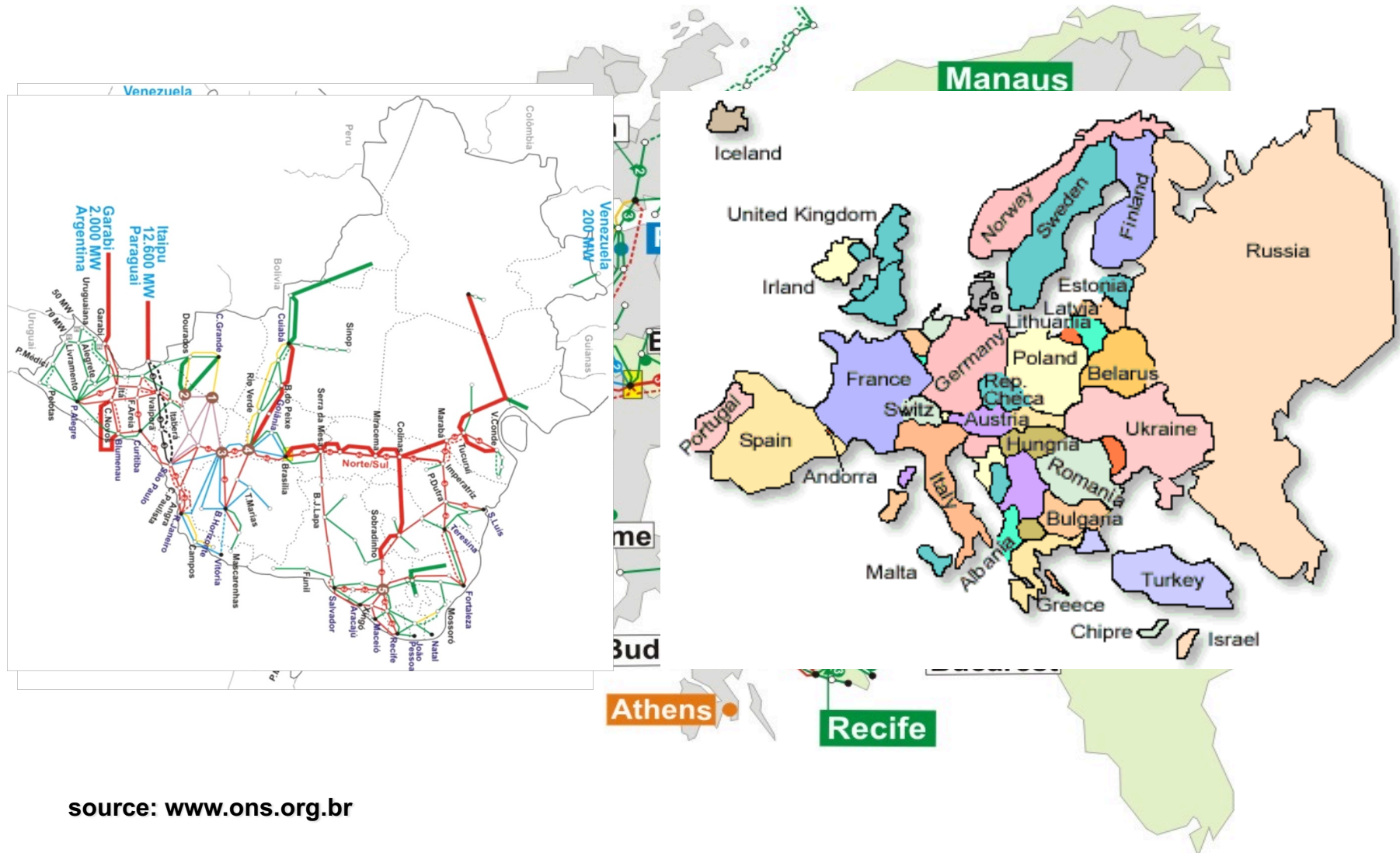
- Brazil is the largest country in South America and the 5th in the world
- 8th largest economy
- The population is approximately 212M
- Rich and diverse landscape with mountains, dense forests and major population centers



São Paulo
(14.7 M)



Dimension of the Country



source: www.ons.org.br

The Brazilian Electric Power System

Background

- Before 1996 the **power sector was verticalized**
- The majority of assets were owned by the government
- Significant **inefficiency, lack of investments** and deterioration of the existing infrastructure
- Following the lead from England and Chile, Brazil took a **deep dive into deregulation** of the power sector

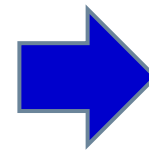


**Private
investments**

+

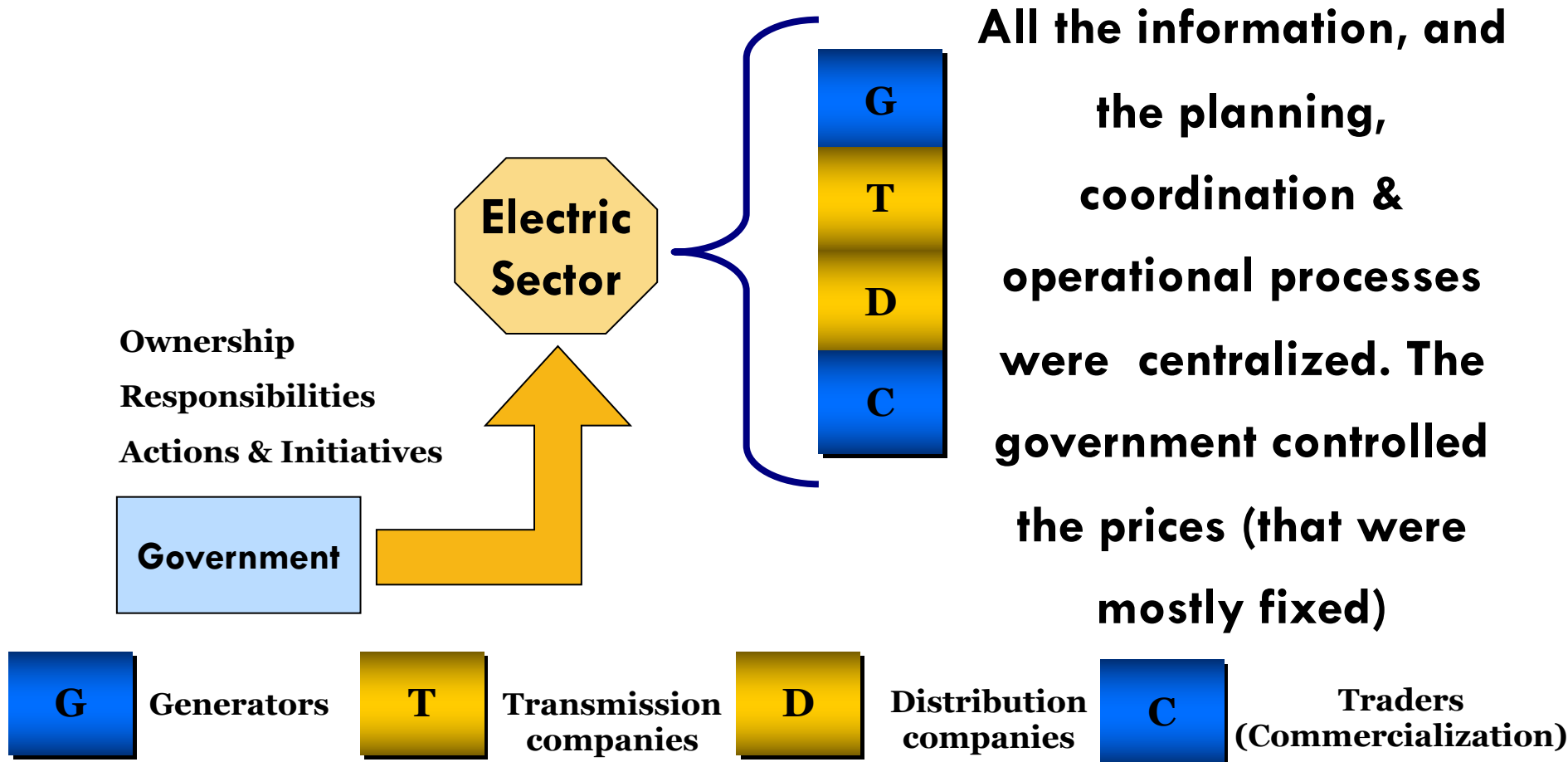


**Promote
Competition**



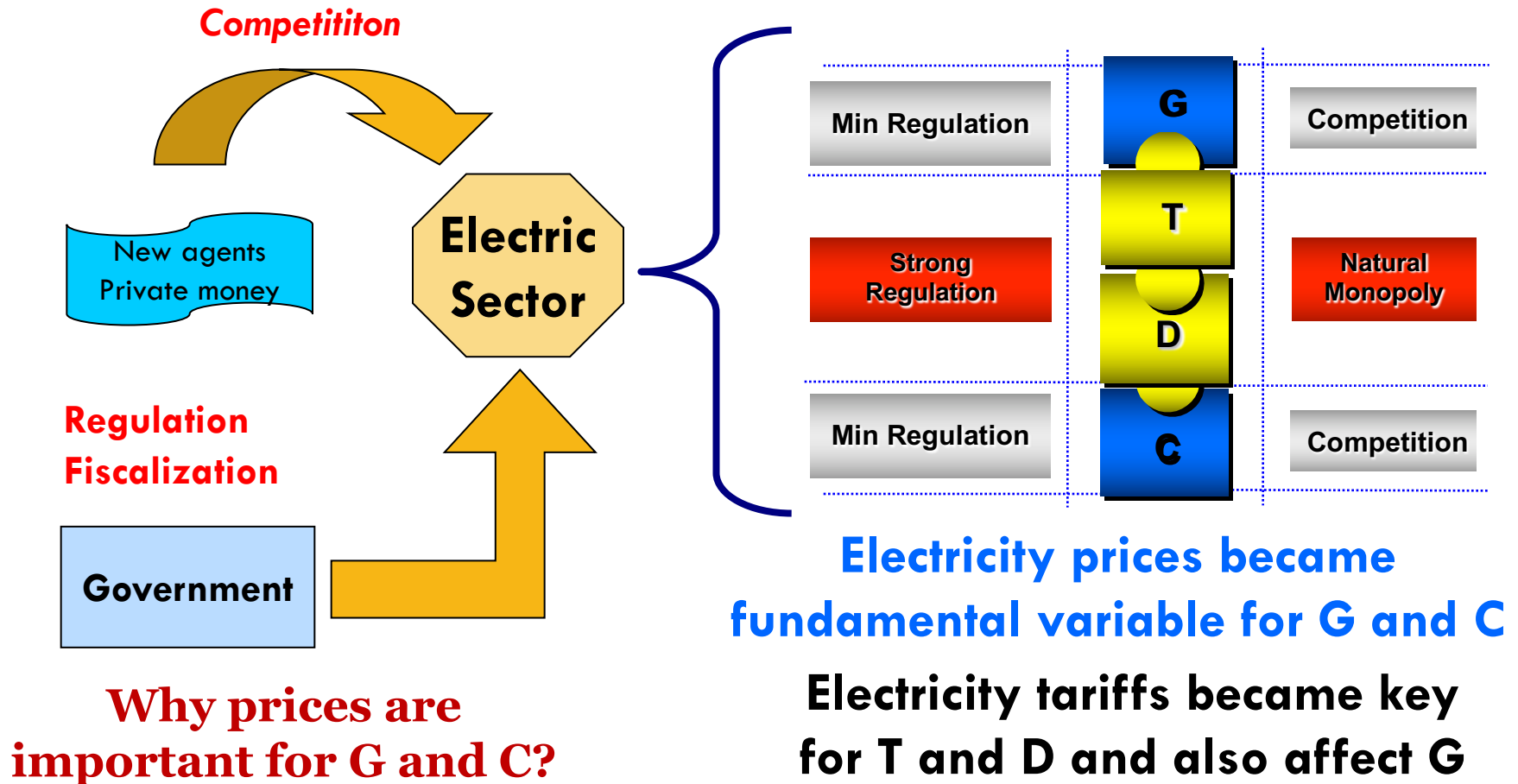
Deregulation of the Electric Sector

Electric sector model before 1996

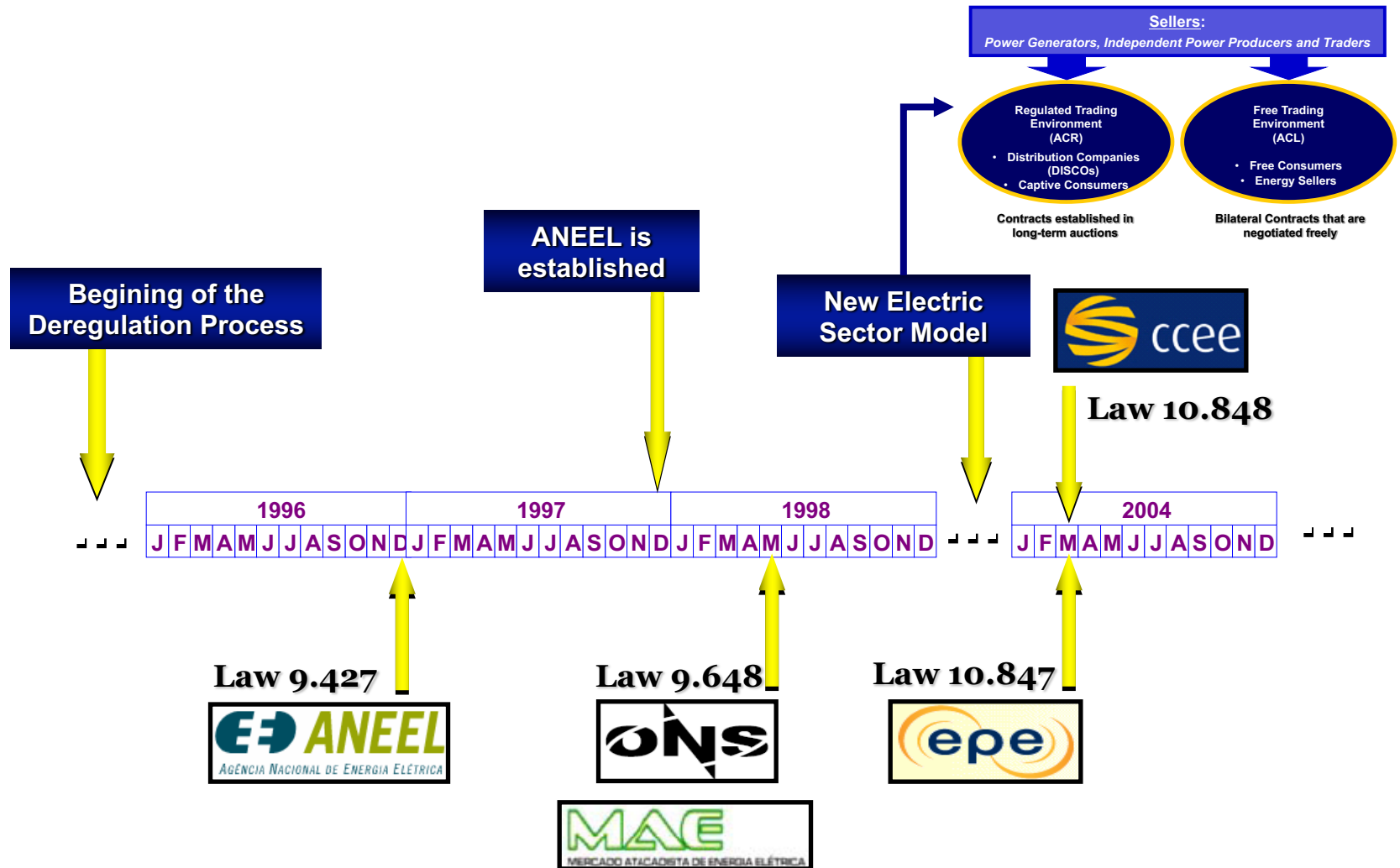


Deregulation of the Electric Sector (cont.)

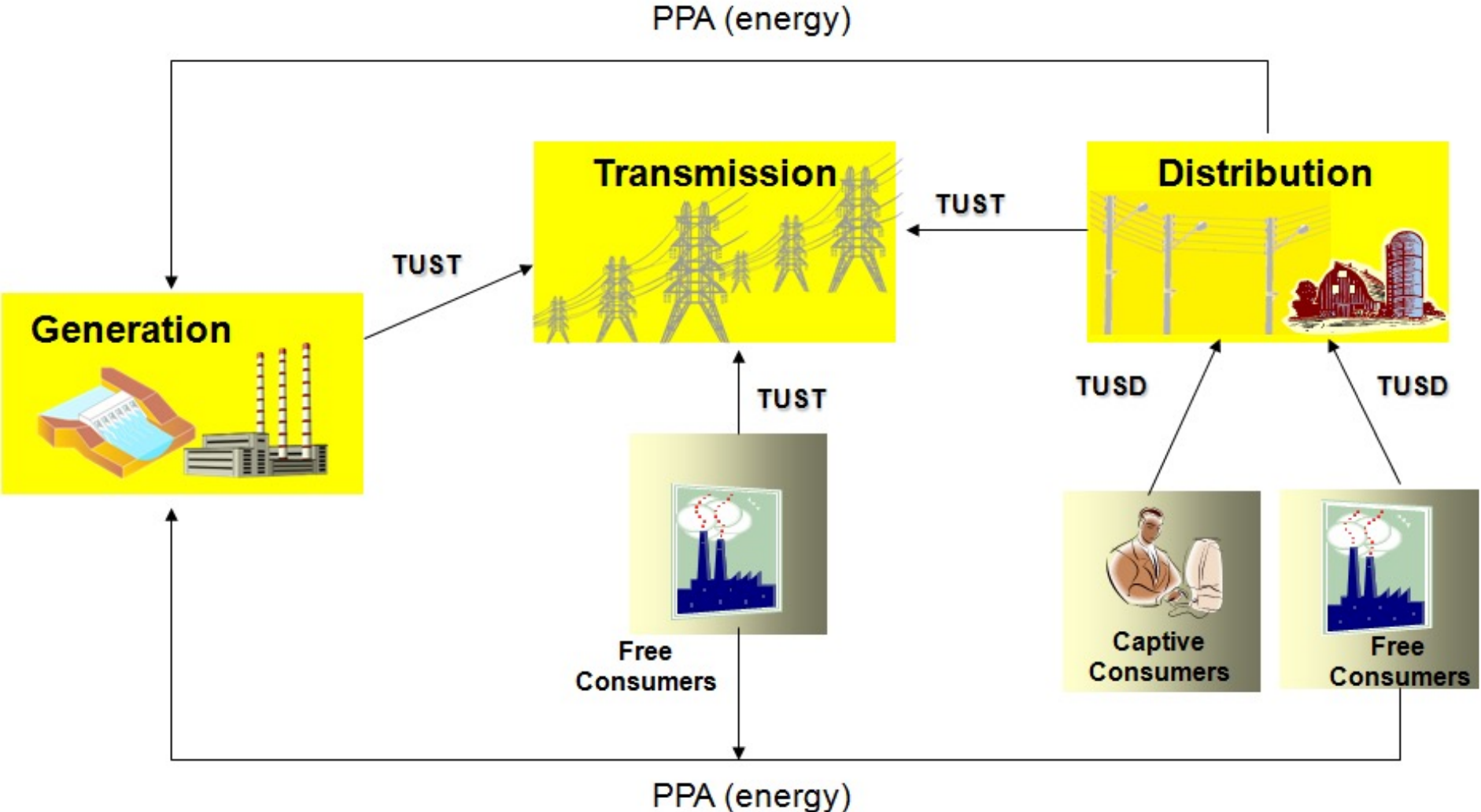
Electric sector model after 1996



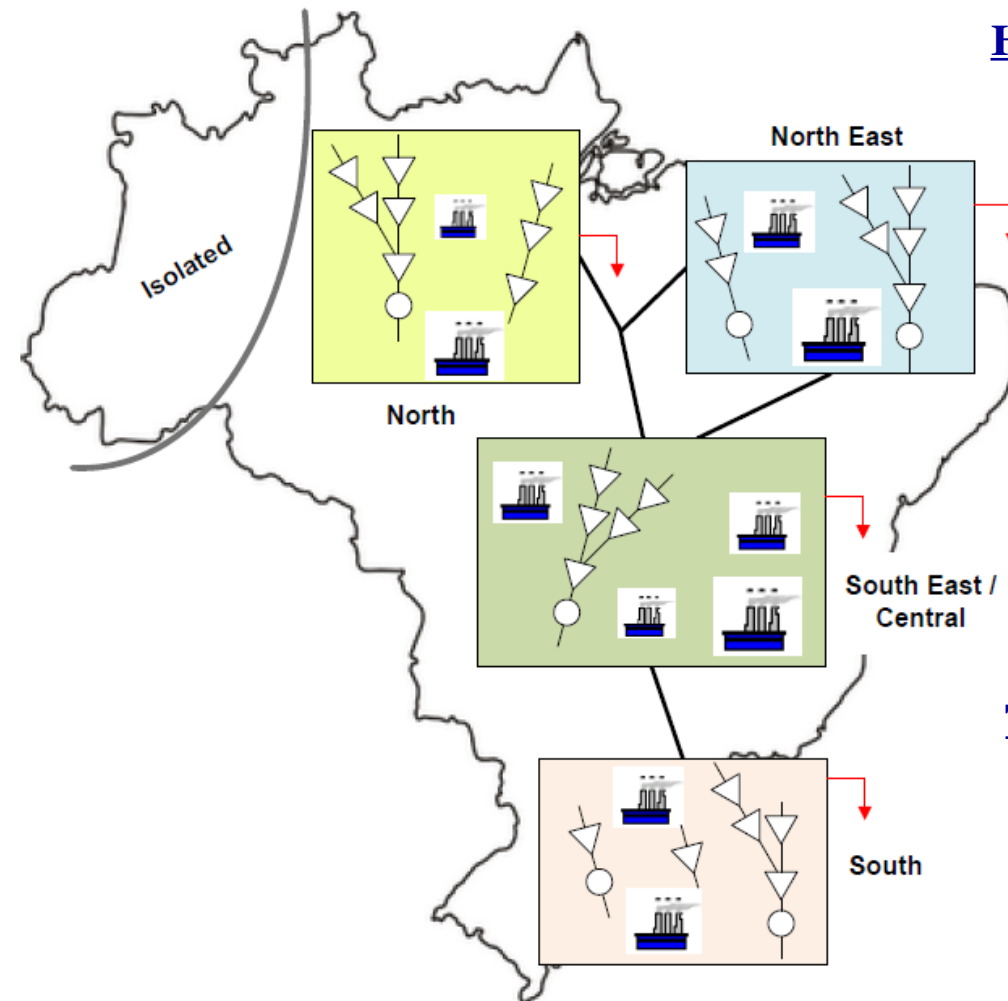
Electric Sector Milestones



Relationships Among Agents



Brazilian Interconnected Power System (SIN)



Hydropower plants

- Represent \cong 68% of the generation capacity
- Concentrated in 12 river basins
- Far away from load centers

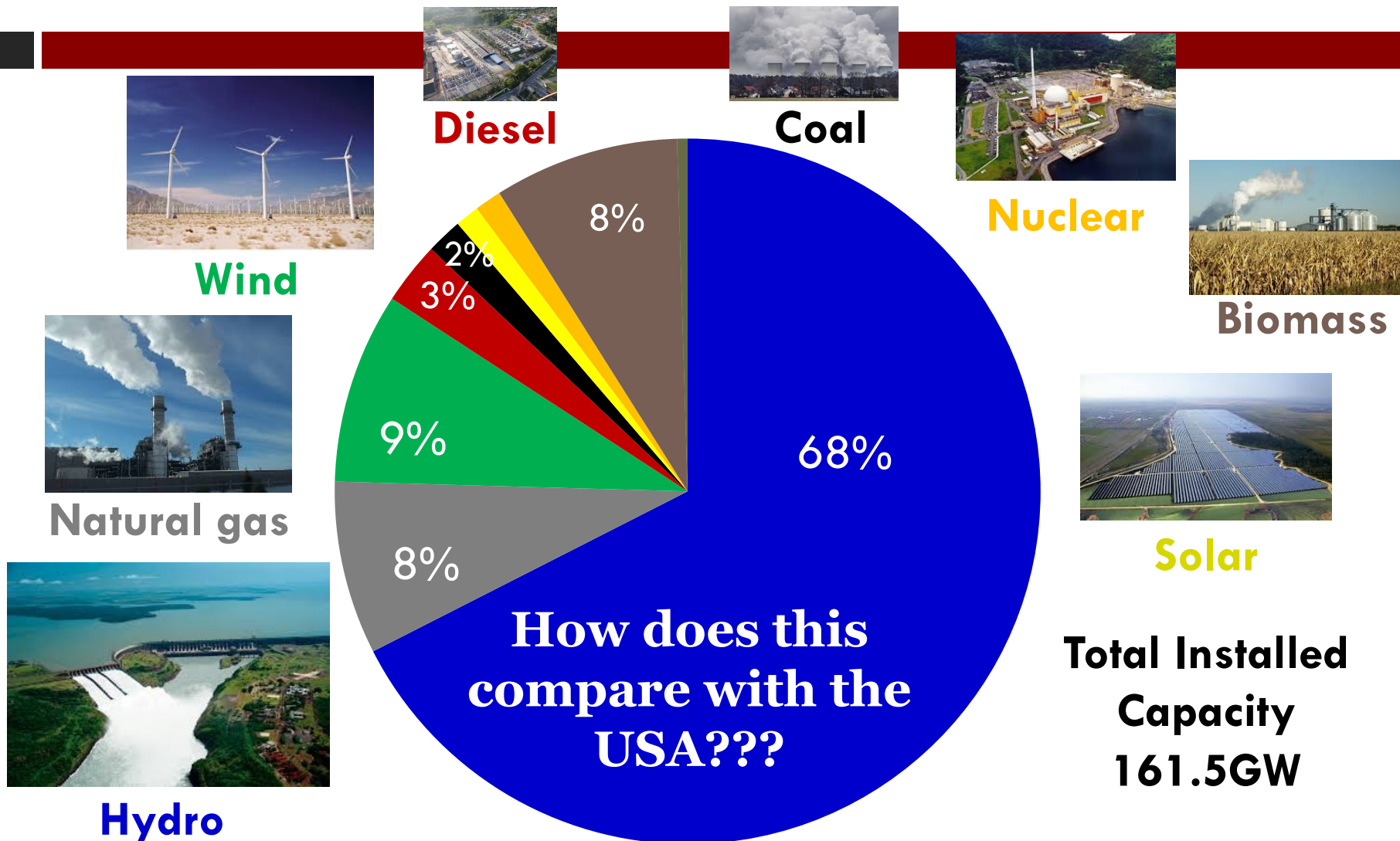
Thermal plants

- Represent \cong 14% of the generation capacity
- Near load centers
- Complement hydro and other sources

Transmission network

- Integrate resources
- Allow for international exchanges
- Enable resource optimization

Electricity Generation Capacity in 2018



■ Hydro ■ Ngas ■ Wind ■ Oil & Diesel ■ Coal ■ Solar ■ Nuclear ■ Biomass ■ Other

Brazilian Interconnected Power System (SIN)

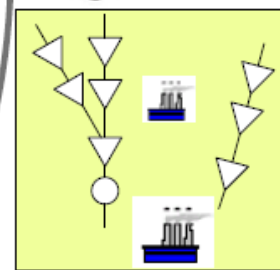
North (N)

- Energy exporter
- New run-of-river hydro
- Tendency to increase exports

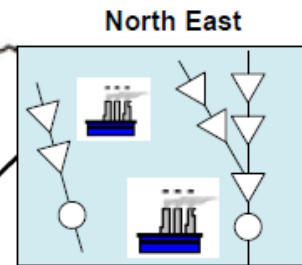
7.6%

**Electricity
Generation - 2018**

581.9 [TWh]



North

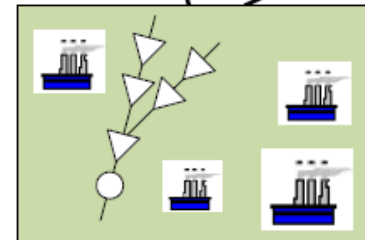


North East

Northeast (NE)

- ↑ electricity demand
- ↑ Wind Farms
- Import from SE

16.3%

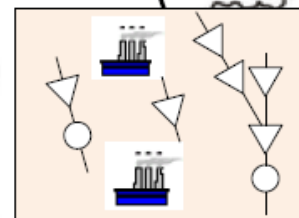


South
Ce

Southeast / Central (SE)

- Largest load centers
- Energy importer
- Capabilities to store electricity

58.7%



South

17.4%

South (S)

- Run-of-river plants (mostly)
- Export to SE
- Interconnection with Argentina

Load - 2018
63.8 [GWavg]

Transmission Interconnections

Transmission Interconnection Capacities

SE – S: 16.3 GW

SE – NE: 9.7 GW

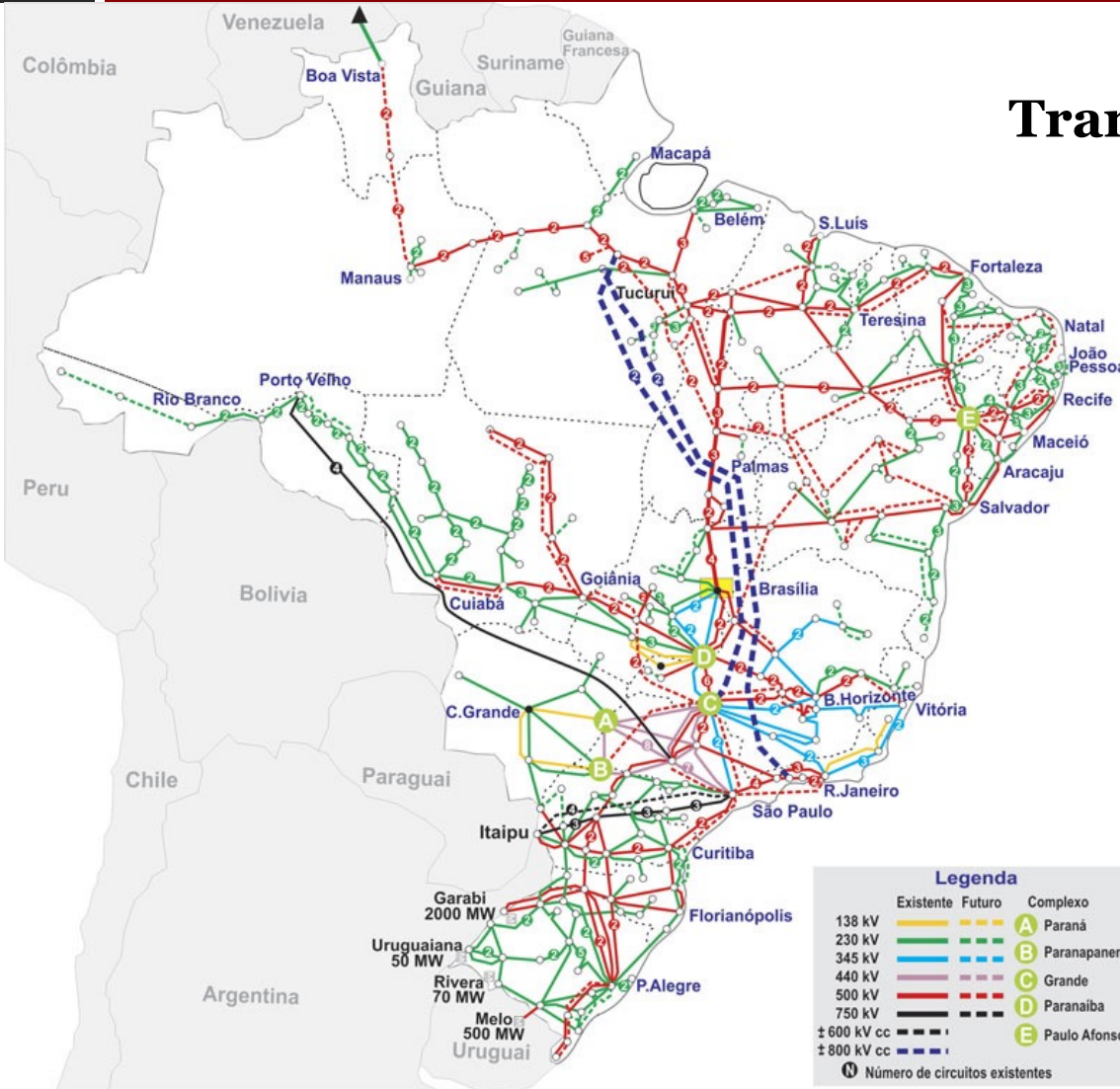
SE – N: 17.9 GW

NE – N: 12.5 GW

**> 141,000 km of
high voltage
transmission lines**

**How many tours
around the world?**

source: www.ons.org.br



Coordination and Optimization of Resources

Renewables Integration

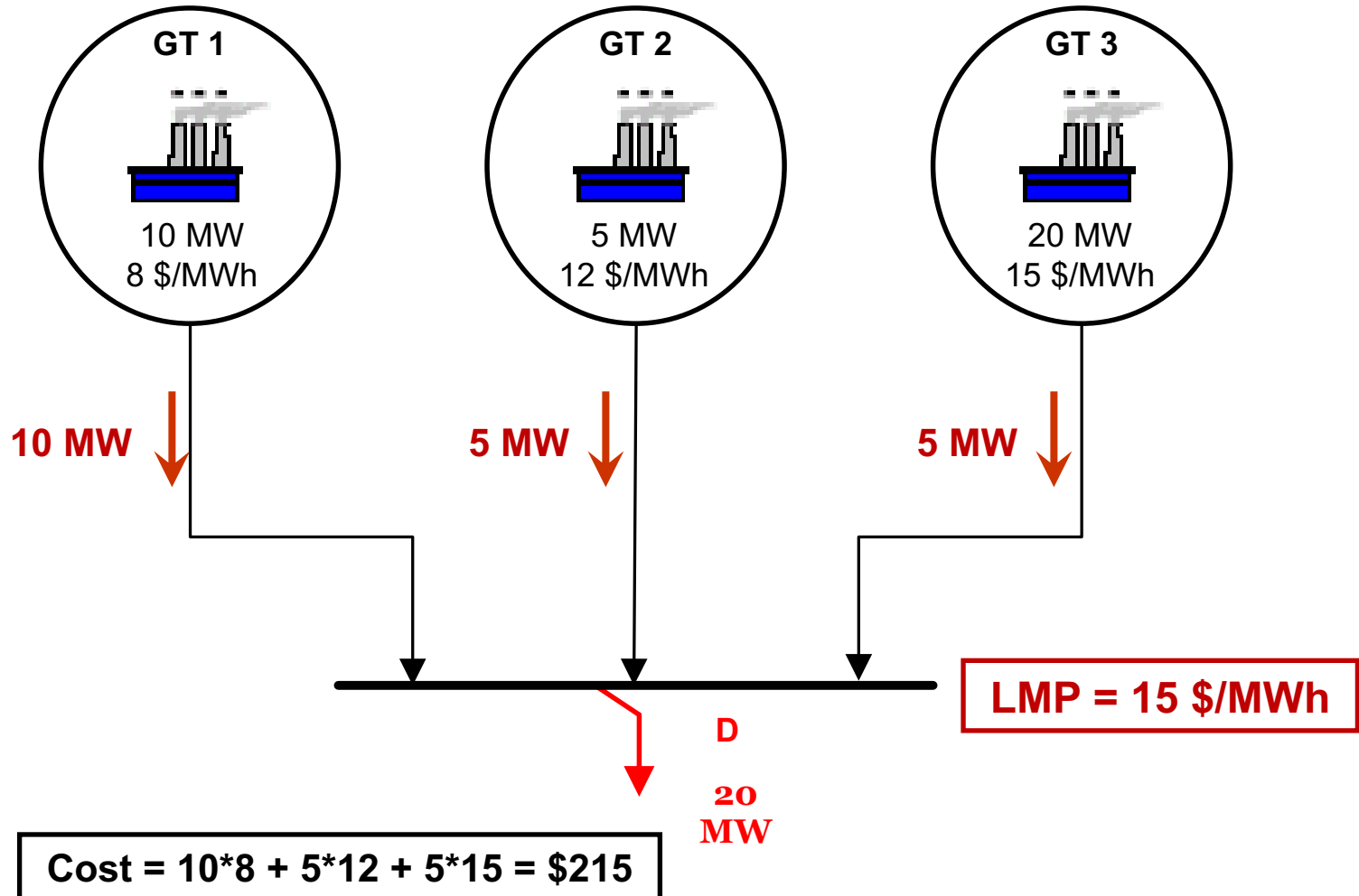
- **Renewable power** sources became a key aspect around the world by **disrupting old frontiers**
- These energy sources are linked to **sustainable development** that is one of the main goals of the modern society these days
- **The raise of renewable power installed** capacity demands new studies about its effects
- **Modeling and decision making techniques** are essential for operational and planning actions



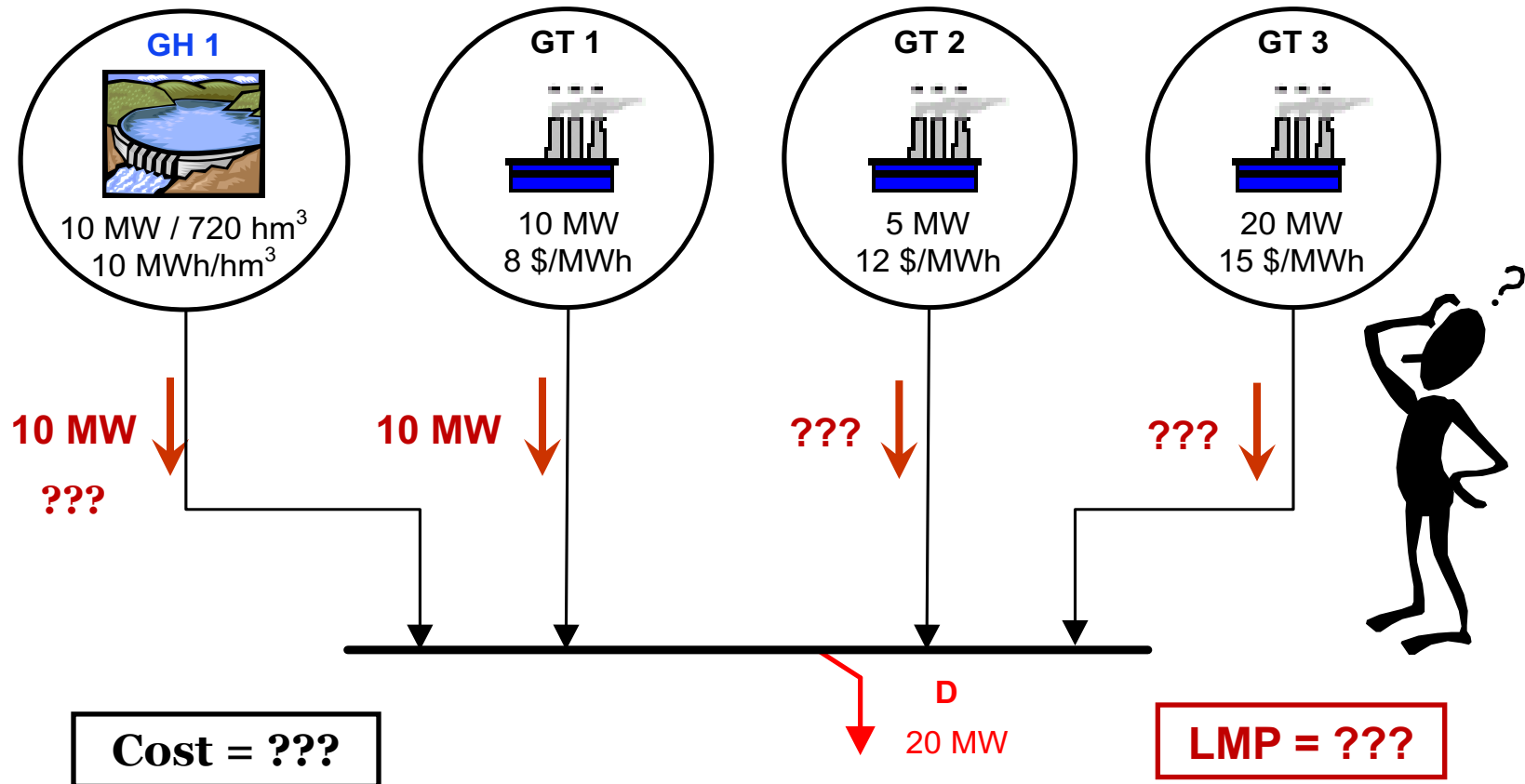
Coordination of Resources

- The main problem with renewable power is its dependence on natural resources (**may not be available when necessary**)
- Hydropower is an exception of these restrictions, since **reservoirs can store water and control generation**
- Countries such Brazil, Norway, Canada and also USA regions (BPA concession area, Western Texas) present **highly dominant renewable generation matrix**
- In this context one important problem addressed in many places is the **hydro-thermal coordination problem (HTCP)**, and its variations to accommodate other renewables

Economic Dispatch – Thermal



Hydro-thermal Coordination (2stages)



$$\text{Cost}_{t_1} = 10 * 0 + 10 * 8 = \$80$$

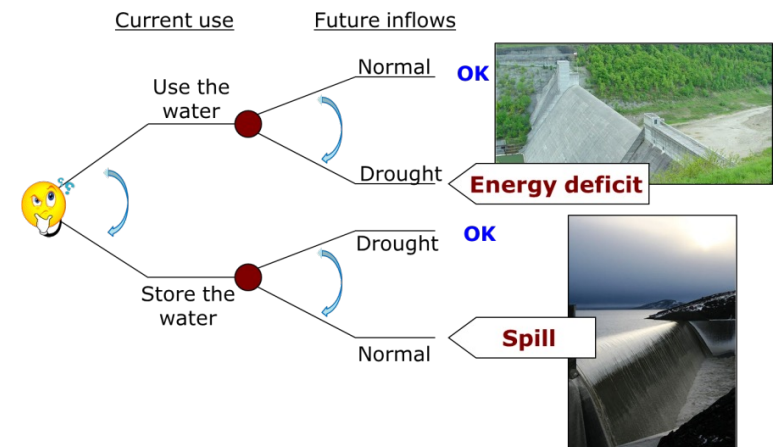
$$\text{Cost}_{t_2} = 10 * 8 + 5 * 12 + 5 * 15 = \$215$$

$$\text{Cost}_{t_1} = 5 * 0 + 10 * 8 + 5 * 12 = \$140$$

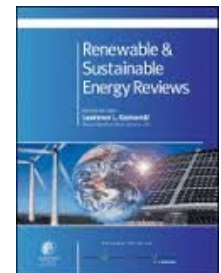
$$\text{Cost}_{t_2} = 5 * 0 + 10 * 8 + 5 * 12 = \$140$$

Stochastic Hydro-thermal Coordination

- Find the sequence of **hydro releases** and **thermal plant dispatches** for a planning horizon to match system demand
 - Resource management
 - Input variable forecasting
 - Operational aspects
- Basic economic criterion
 - **Minimize operational costs** (present + expected future)
- Usually modeled and solved using stochastic programming (optimization) techniques



de Queiroz, A.R., (2016) Stochastic Hydro-thermal Scheduling Optimization: An Overview, Renewable and Sustainable Energy Reviews, 62: 382-395



A Little About Stochastic Programming

- **Stochastic programming** (SP) is used as a tool for modeling **optimization** problems under **uncertainty**
- This operations research area was born in the 1950s “Linear programming under uncertainty” (**Dantzig, 1955**)



VOLUME 1
NUMBERS 3 AND 4
April–July 1955

Management
Science



Power generation scheduling

- Real problems constantly include parameters that are unknown when decisions should be made
- SP models rely on the assumption that **probability distributions** are known or can be estimated
- There are different classes of SPs, and our focus is on **multi-stage stochastic linear programs** (SLP-t)

Epidemic control

- Decisions have to be made at different time stages and there is a dynamic link between stages

Transportation planning

Variables & Parameters

□ Sets:

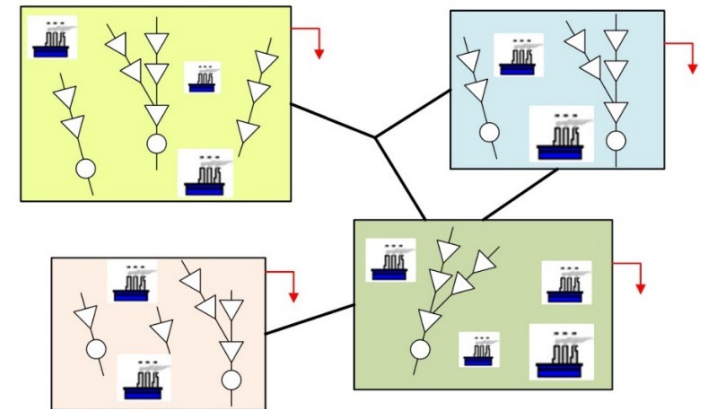
- Set of **hydro power plants**: $i \in I$
- Set of **thermal power plants**: $\ell \in L$
- Set of time stages: $t \in T$
- Set of electrical **subsystems**: $r \in R$
- Set of **curtailment levels**: $k \in K$
- Subset of upstream reservoirs: M_i

□ Decision variables:

- **Hydro generation**: GH_i^t
- **Spilled volumes**: S_i^t
- **Water volume storage**: x_i^t
- **Thermal generation**: GT_ℓ^t
- **Energy transfers between regions**: $F_{r r'}^t$
- **Load curtailment**: GD_k^t

□ Parameters:

- Future water inflows: b_t, b_{t+1}, \dots, b_T (**uncertainty**)
- Electricity demand at region r : D_{tr}
- Bound limits: \underline{x}, \bar{x}



HTCP Model Formulation for Stage-t

$$h_t(x^{t-1}, b_t^\omega) = \min \underbrace{\sum_{\ell \in L} c_\ell^t GT_\ell^t + \sum_{k \in K} u_k^t GD_k^t}_{\text{Present Cost}} + \underbrace{\frac{1}{(1 + \beta)} \mathbb{E}_{b_{t+1}|b_1, \dots, b_t} h_{t+1}(x^t, b_{t+1})}_{\text{Expected Future Cost}}$$

Water Balance

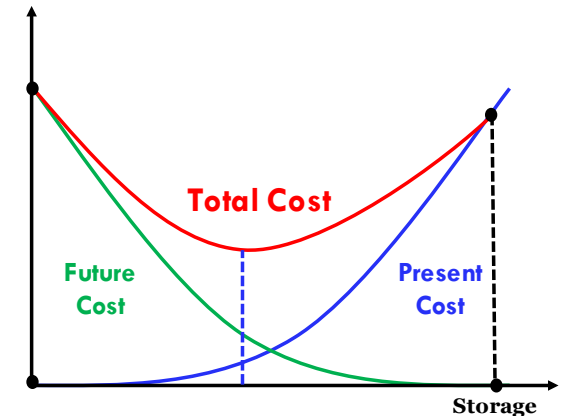
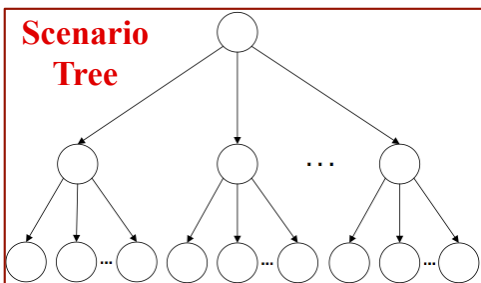
$$\text{s. t. } x_i^t + GH_i^t + S_i^t = x_i^{t-1} + b_{t+1}^\omega + \sum_{j \in M_i} (GH_j^t + S_j^t) \quad \forall i \in I$$

Demand Satisfaction

$$\sum_{i \in I_r} \rho_i GH_i^t + \sum_{\ell \in L} GT_\ell^t + \sum_{k \in K} GD_k^t - \sum_{\substack{r' \in R \\ r' \neq r}} F_{r r'}^t + \sum_{\substack{r' \in R \\ r' \neq r}} F_{r' r}^t = D_{tr} \quad \forall r \in R$$

Simple Bounds

$$\begin{aligned} \underline{x}_i^t &\leq x_i^t \leq \bar{x}_i^t && \forall i \in I \\ 0 &\leq GH_i^t \leq \overline{GH}_i^t && \forall i \in I \\ 0 &\leq S_i^t && \forall i \in I \\ \underline{GT}_\ell^t &\leq GT_\ell^t \leq \overline{GT}_\ell^t && \forall \ell \in L \\ 0 &\leq GD_k^t && \forall k \in K \\ 0 &\leq F_{r r'}^t \leq \overline{F}_{r r'}^t && \forall (r, r') \in R \end{aligned}$$



HTCP Model with Wind Penetration

$$\begin{aligned}
 h_t(x^{t-1}, b_t^\omega) = & \min \sum_{\ell \in L} c_\ell^t GT_\ell^t + \sum_{k \in K} u_k^t GD_k^t + \frac{1}{(1 + \beta)} \mathbb{E}_{b_{t+1}|b_1, \dots, b_t} h_{t+1}(x^t, b_{t+1}) \\
 \text{s. t. } & x_i^t + GH_i^t + S_i^t = x_i^{t-1} + b_{t+1}^\omega + \sum_{j \in M_i} (GH_j^t + S_j^t) \quad \forall i \in I \\
 & \sum_{i \in I_r} \rho_i GH_i^t + \sum_{\ell \in L} GT_\ell^t + \sum_{k \in K} GD_k^t - \sum_{\substack{r' \in R \\ r' \neq r}} F_{r r'}^t + \sum_{\substack{r' \in R \\ r' \neq r}} F_{r' r}^t = D_{tr} \quad \forall r \in R \\
 & \sum_{v \in V_r} w_v^t \\
 & w_v^t \leq n \frac{1}{2} \sigma \cdot A \cdot w S_{vt}^\omega{}^3 \cdot C_p^t \quad \forall v \in V
 \end{aligned}$$

Present Cost
Future Cost Function

Water Balance

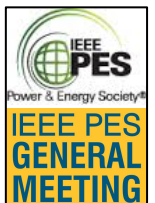
Demand Satisfaction

Maximum wind power generation

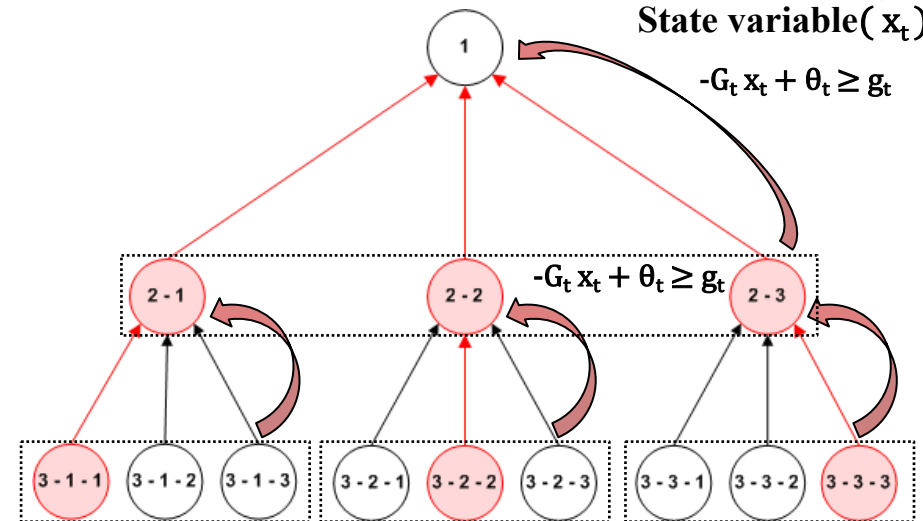
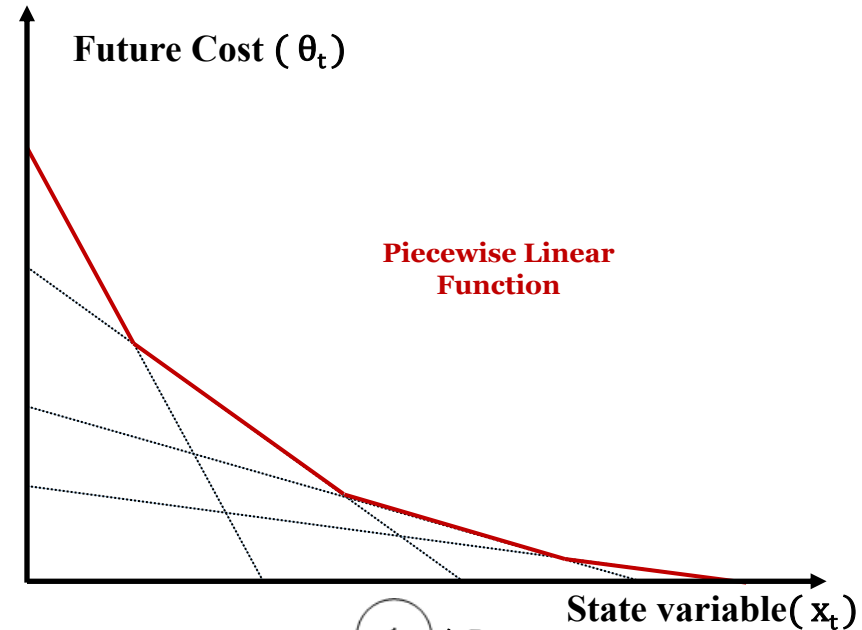
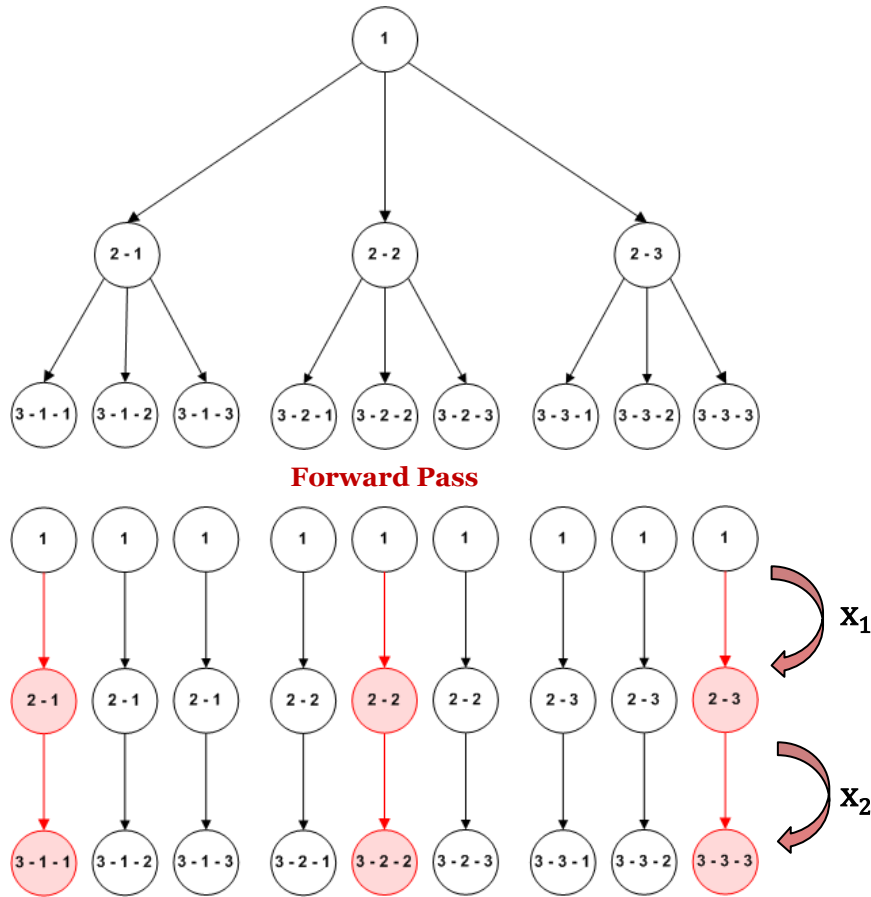
Simple bounds

Silva, S.R., de Queiroz, A.R., Lima, L.M.M., Lima, J.W.M., (2014) Effects of Wind Penetration in the Scheduling of a Hydro-Dominant Power System, IEEE PES General Meeting

Incorporate Solar PV, other storage technologies and handle different uncertainty time scales & operational issues



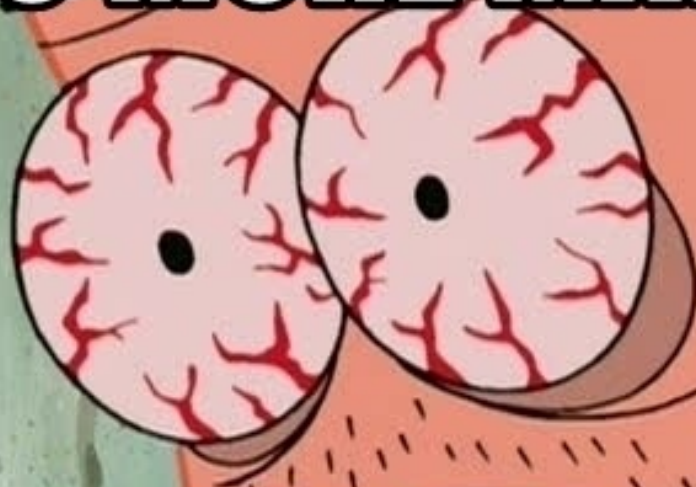
Sampling-based Decomposition Algorithm



de Queiroz, A.R., Morton, D.P., (2013) Sharing Cuts under Aggregated Forecasts when Decomposing Multi-stage Stochastic Programs, Operations Research Lett, 41(3): 311-316



NO MORE MATH



PLEASE...

Pricing Formation in the Electricity Market

The Brazilian Electricity Market

Sellers:

Power Generators, Independent Power Producers and Traders

Regulated Trading Environment (ACR)

- Distribution Companies (DISCOs)
- Captive Consumers

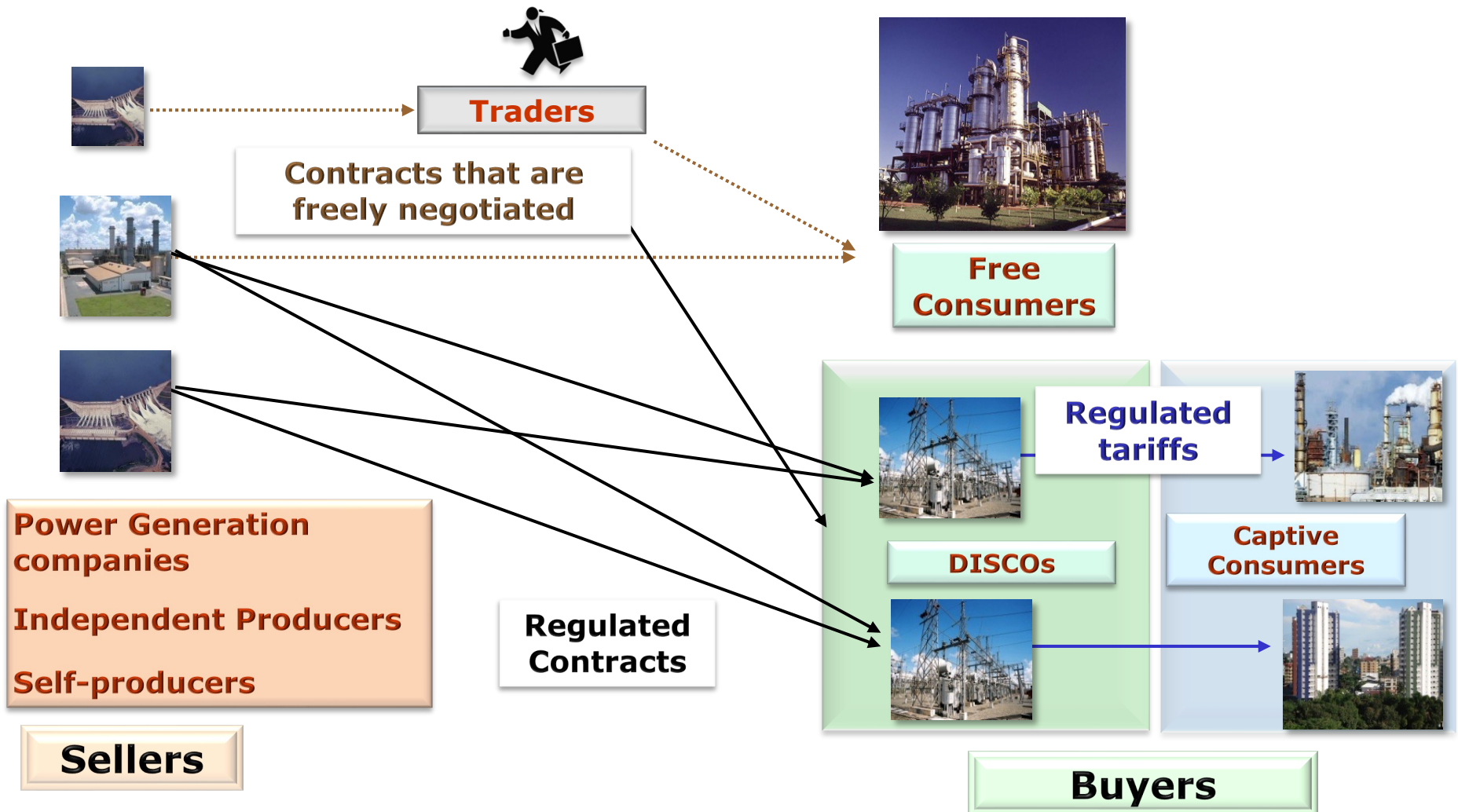
Contracts established in long-term auctions

Free Trading Environment (ACL)

- Free Consumers
- Energy Sellers

Bilateral Contracts that are negotiated freely

Market Configuration



Regulated Market: Long-term Contracts

- **In the Regulated Market**, DISCOs ($\cong 70\%$ of the market) buy electricity through contracts in **long-term auctions** (backed by assured energy)
 - ▣ This process is established for different reasons (promote new investments “**new energy**”, sell expired contracts “**existing energy**”, **promote matrix diversification**)
 - ▣ The DISCOs have to contract 100% of their future demand projections (up to five years ahead)
 - ▣ A mix of prices is formed and applied to the captive consumers (**regulated electricity tariffs**)

“New” vs “Existing” Energy in Auctions

- Separate auctions for purchasing “**new energy**” (generation expansion) and “**existing**” (supply of the current market)
- Reasons for the different auctions
 - Offer contracts with **longer duration** for new generation
 - Offer contracts with **shorter duration** for existing generation
 - Management of future uncertainties by the DISCO
 - **Risk sharing** between new and existing generation, providing **flexibility in the management of energy portfolios**

Antes do Leilão: Declaração da Demanda

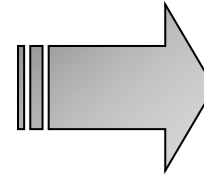
Before the auction each DISCO informs how much they need to hire

DISCO 1

DISCO 2

▪
▪
▪

DISCO n



DISCO 1

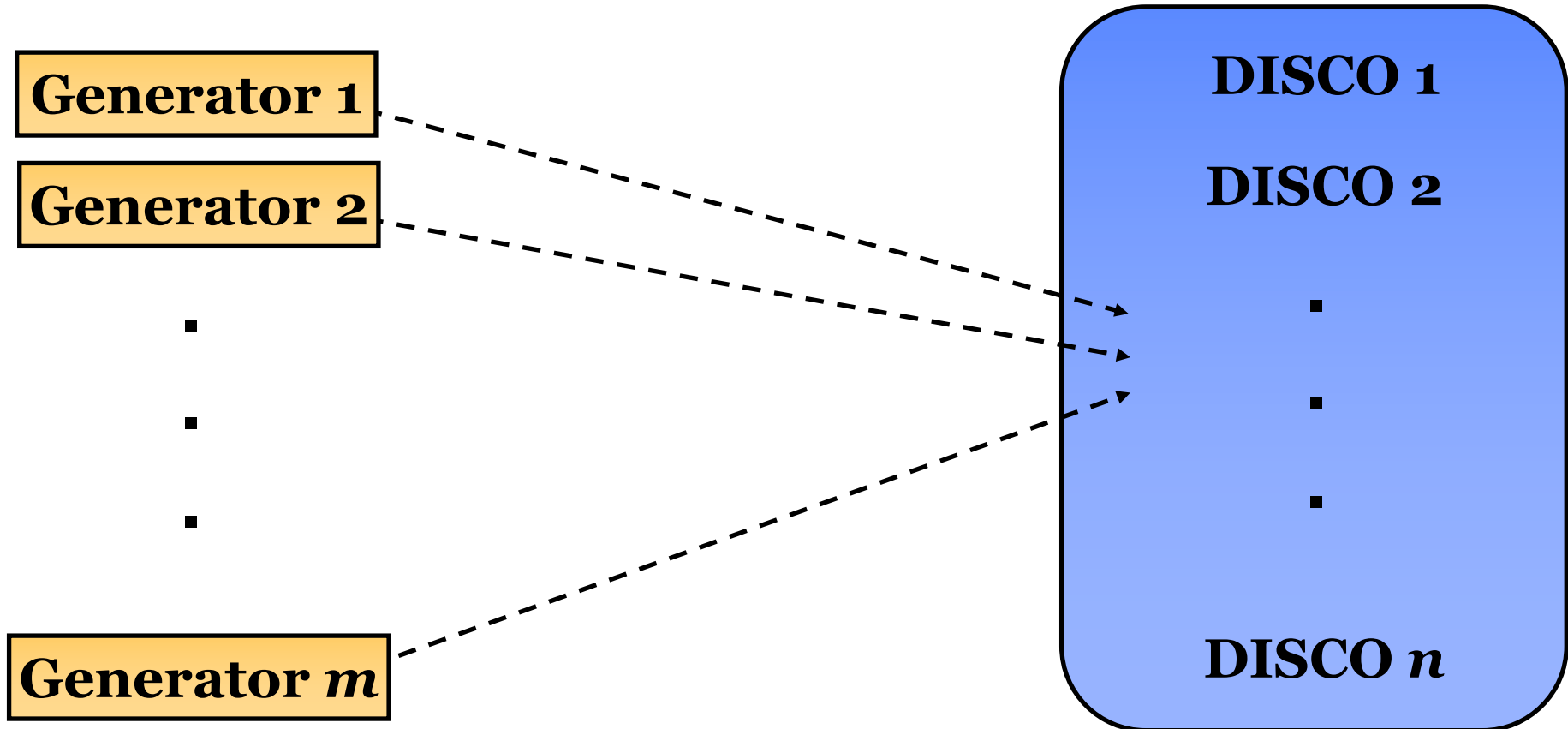
DISCO 2

▪
▪
▪

DISCO n

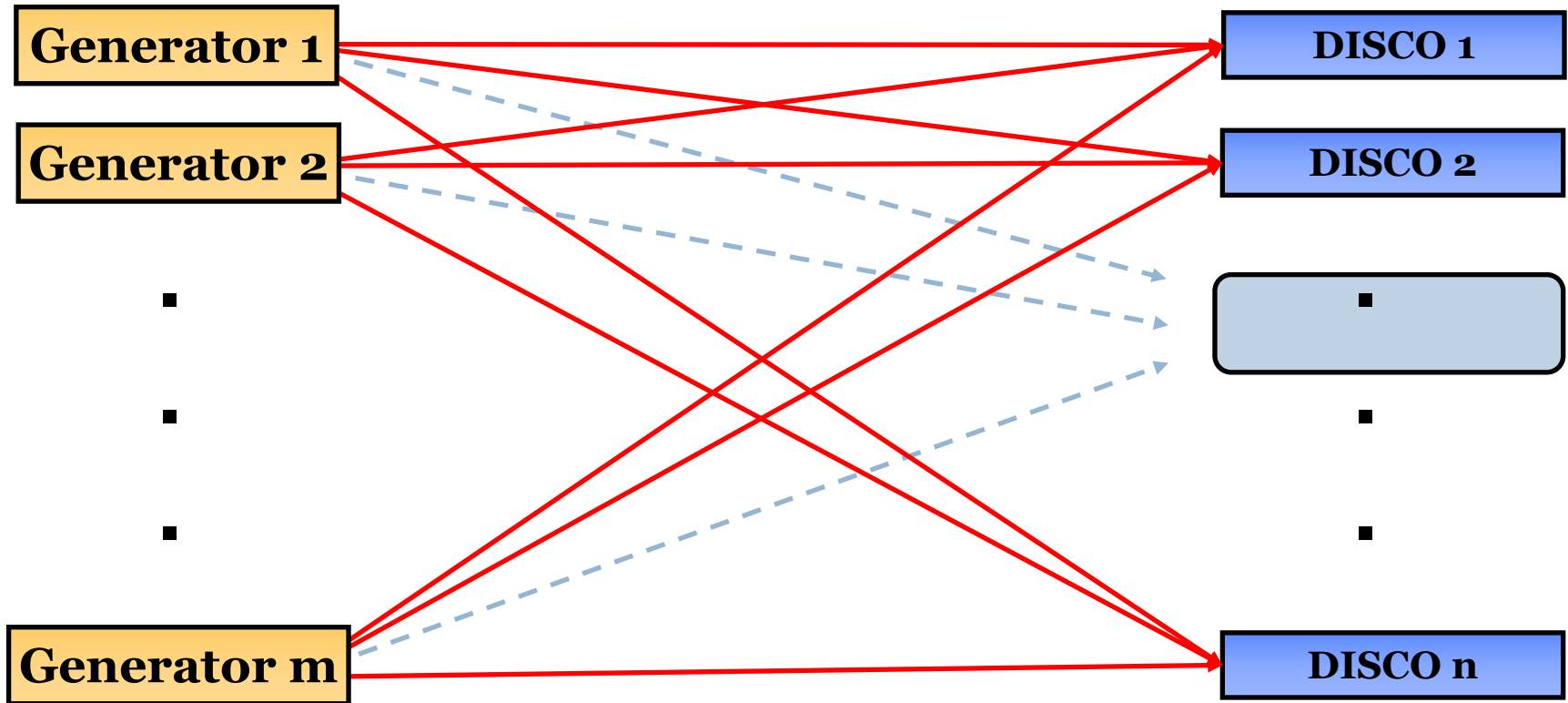
The total amount informed by each DISCO and the total amount of the pool of DISCOs is not revealed before or during the auction

During the Auction – Demand Satisfaction



**An auction to hire “x” MWavg is performed
In the auction, gerators make price bids to satisfy the demand**

After the Auction: Bilateral Contracts



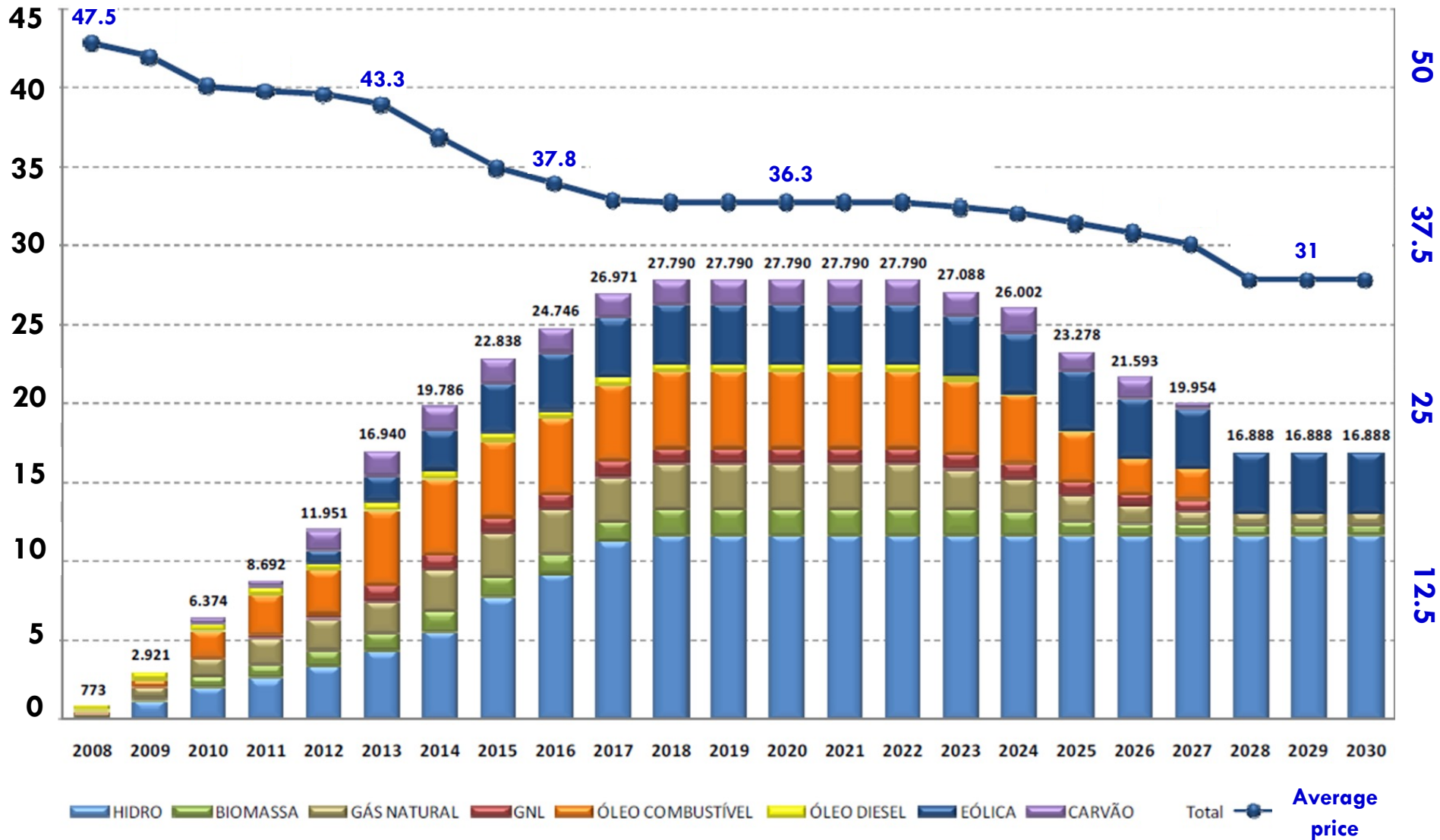
Offers most competitive in terms of price win

Then, bilateral contracts are signed in proportion to the generator offer and the DISCO demand

A Experiência do Brasil: Leilões de Energia Nova

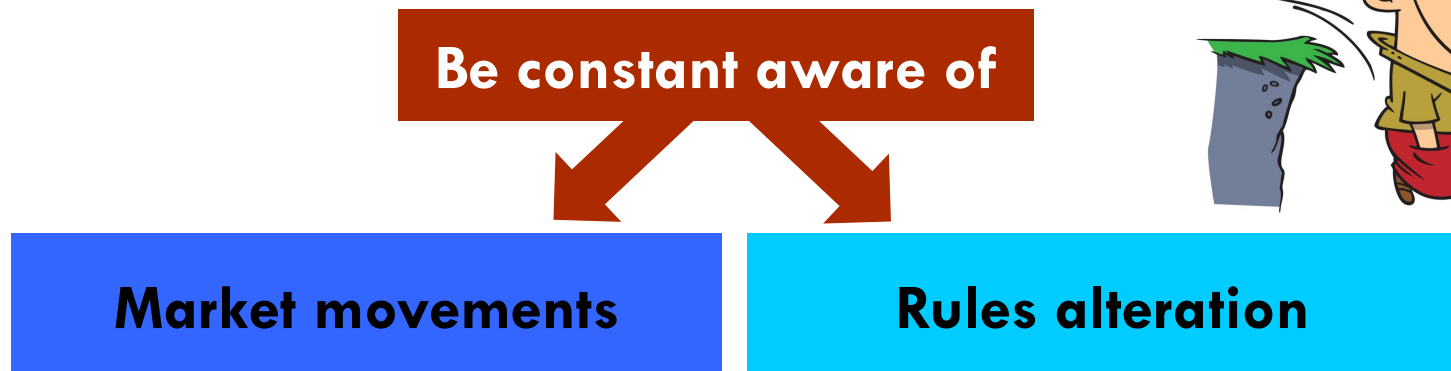
GWavg

US\$/MWh



The Brazilian Free Market

- In the Free Market (ACL), the participants can choose their supplier
- Agents attempt to manage their portfolio
 - ▣ **Minimize costs** or **maximize profits**
 - ▣ Reduce exposition to future risks
- The consumer has to **manage energy usage**

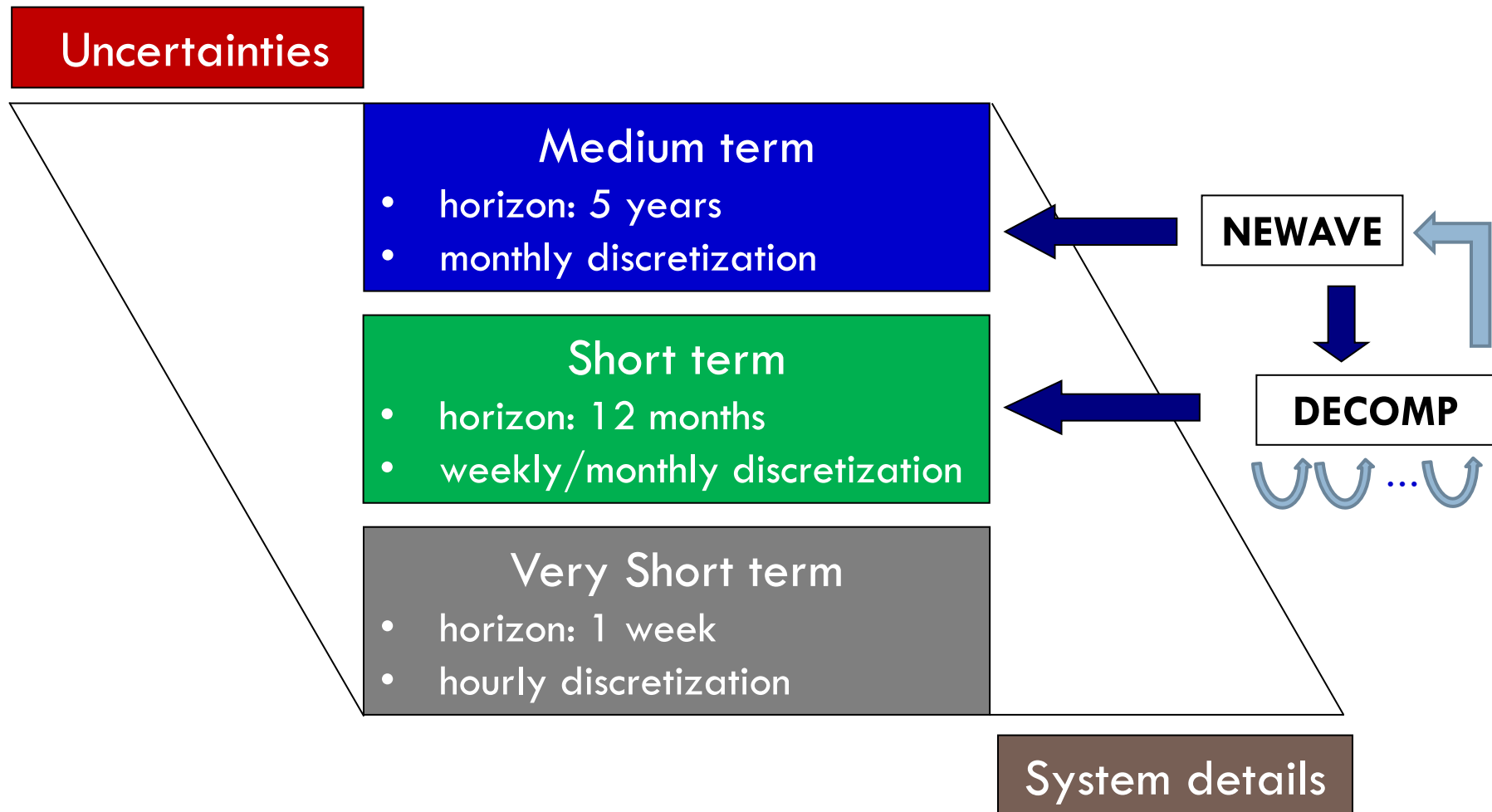


Pricing in the Brazilian Free Market

- The **electricity price in the Free market** is based on results obtained by HTCP optimization models (**NEWAVE e DECOMP**)
- **Methodology** based on “**Tight Pool**”
- Instead of seeking for an equilibrium between supply and demand, the **price is based on** the locational marginal prices (**LMPs**) from the **HTCP optimization**
- Where the goal is to **minimize the total expected operational costs** to satisfy the system demand during the planning horizon

How to find LMPs in a HTCP?

Operational Planning Structure

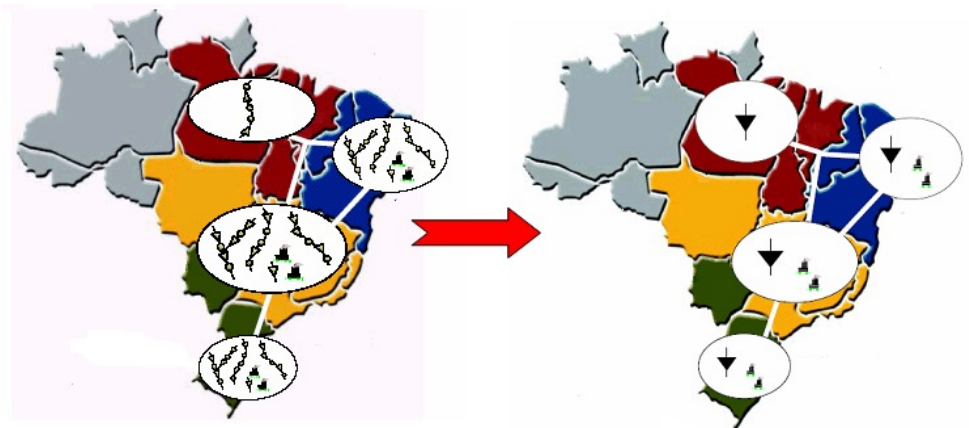


NEWAVE Model

- Used since 1999 in the Brazilian power sector
- **Optimizes the dispatches** of all the power plants (>30MW) from the SIN
- Used **in HTCP** considering **five year horizons** with monthly discretization
- **SDDP** – Stochastic Dual Dynamic Programming
- Determine the Operational policies for the power plants

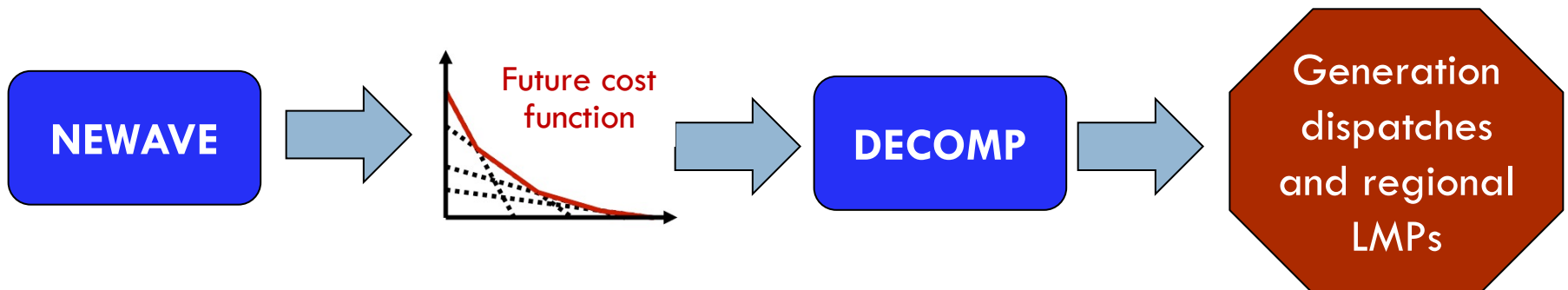
Dimensionality Reduction:

**Aggregated Reservoir
Representation**

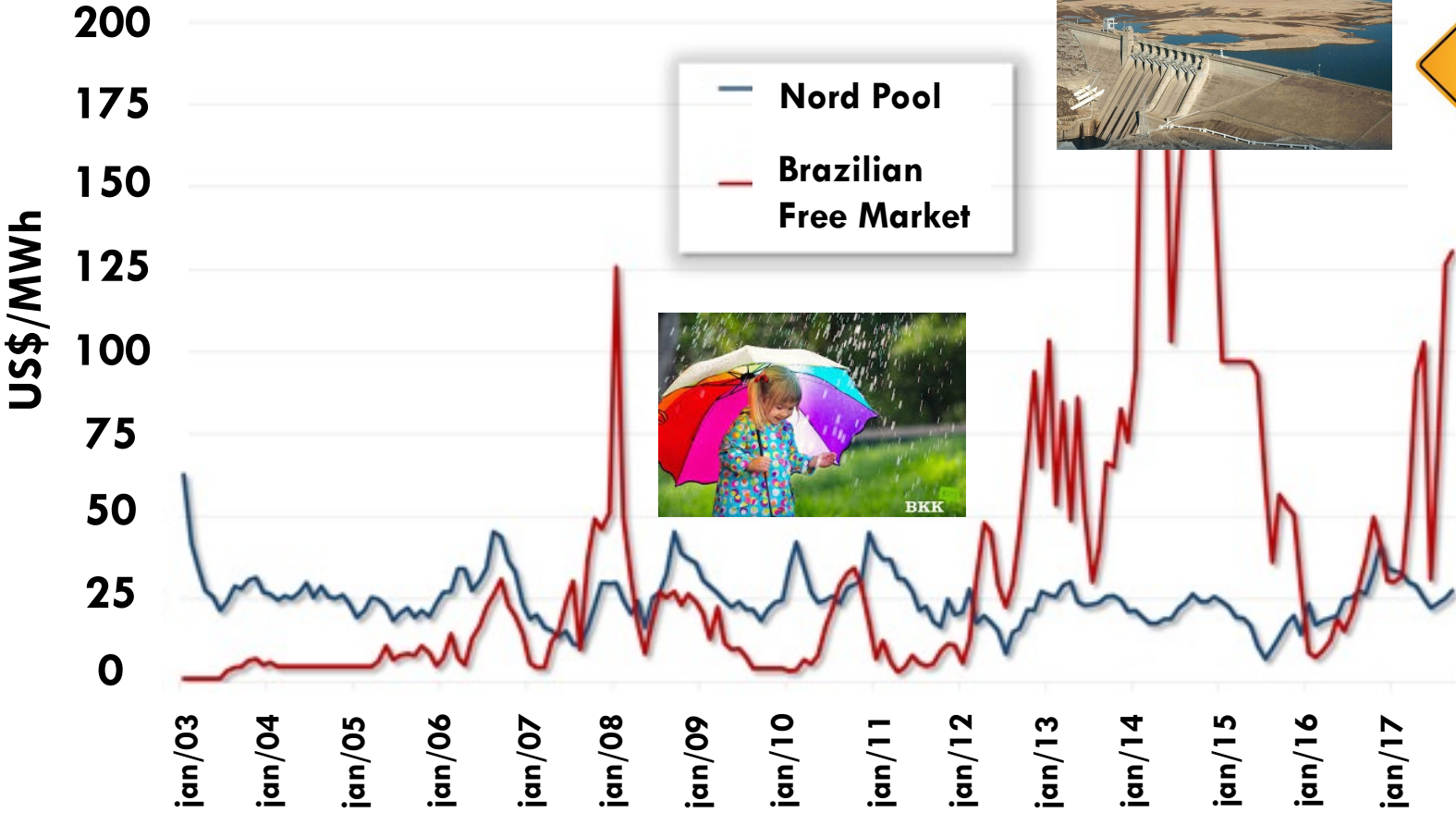


DECOMP Model

- Determine the **short term operation** of the power plants
- Representation of **individual plants** with their associated features
- Defines the **locational marginal prices** for each week
- The goal is to minimize the total operational costs to satisfy demand
- Subjected to **generation** and **transmission** operational constraints
- One year horizon with weekly and monthly discretization

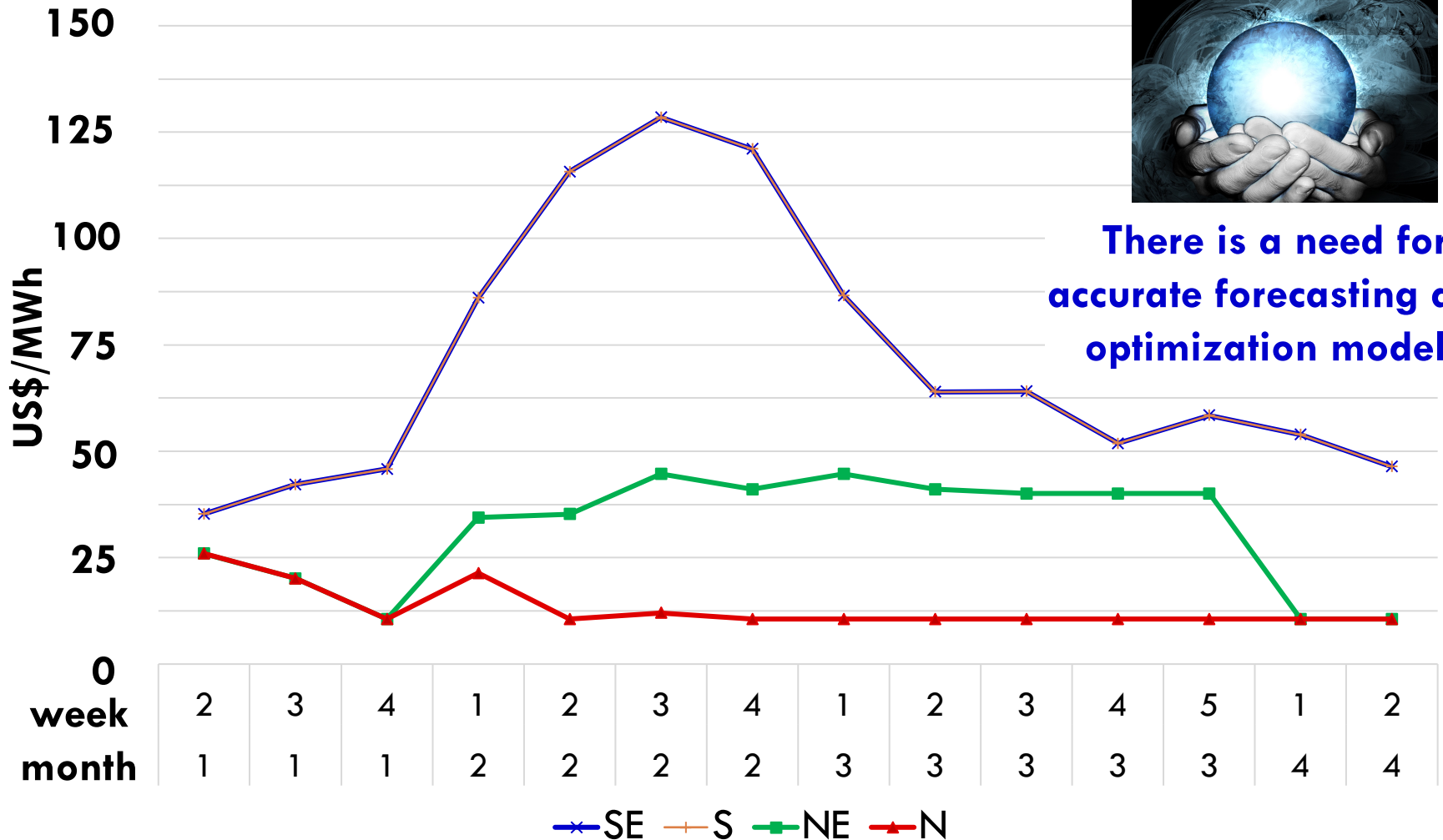


Brazilian Free Market vs Nord Pool - Prices



BKK

Free Market LMPs - 2019



There is a need for accurate forecasting and optimization models

Final Comments

Final Comments

- The **Brazilian electric power sector** was discussed
- The structure of the electricity market was presented
- The HTCP is key in the definition of operational strategies that minimizes operational costs
- The HTCP is used to define prices in the Free Market
- **Analytics** and **Decision-making** techniques are key to support system analysts when defining operations strategies, managing portfolios and planning systems resources



THANK YOU !

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Durham, April 2019

Guest Lecture in Power Markets – Nicholas School of Environment

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