

STOCHASTIC POWER GENERATION SCHEDULING USING TEMOA



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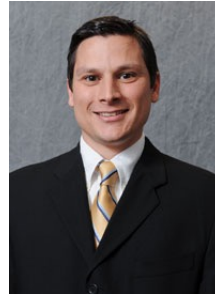
Department of Civil, Construction & Environmental Engineering



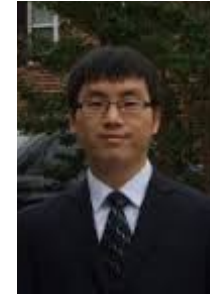
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that we thank...



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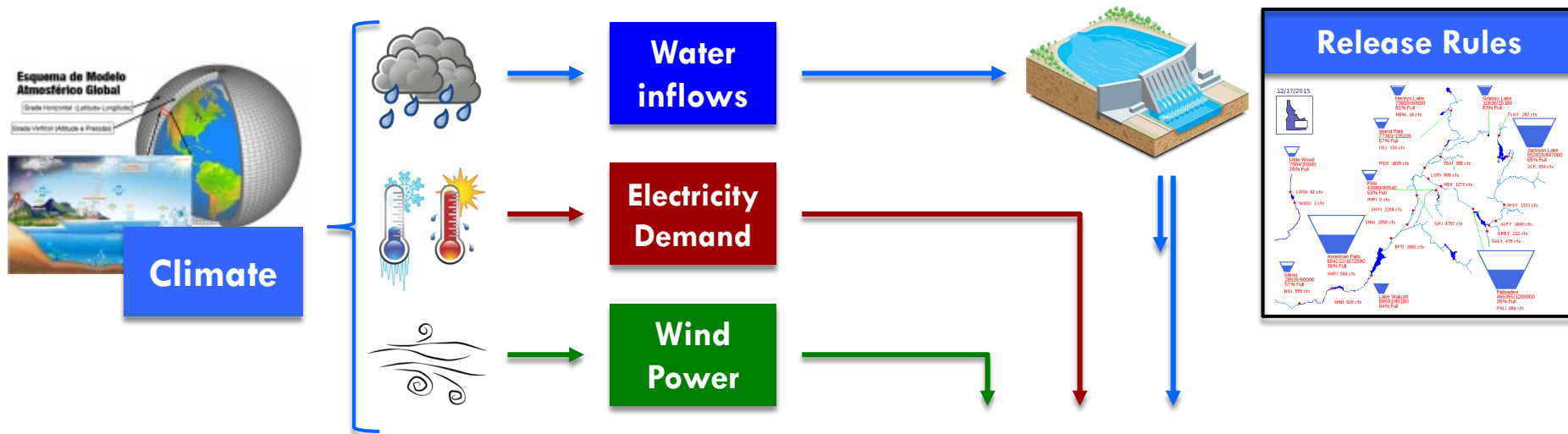
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Overview

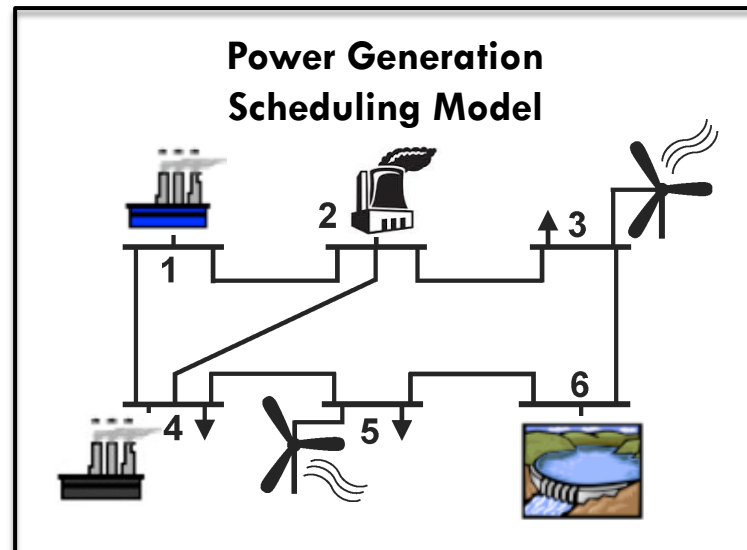
- Introduction
- Tools for Energy Model Optimization and Assessment (TEMOA)
 - ▣ TEMOA's Purposes
 - ▣ General Mathematical Formulation
- From Capacity Expansion to Power Generation Scheduling
 - ▣ Modeling Goals
 - ▣ Enhancing TEMOA Formulation
 - ▣ Stochastic Power Generation Scheduling with TEMOA
- Case Study
- Next Steps & Final Comments

Introduction

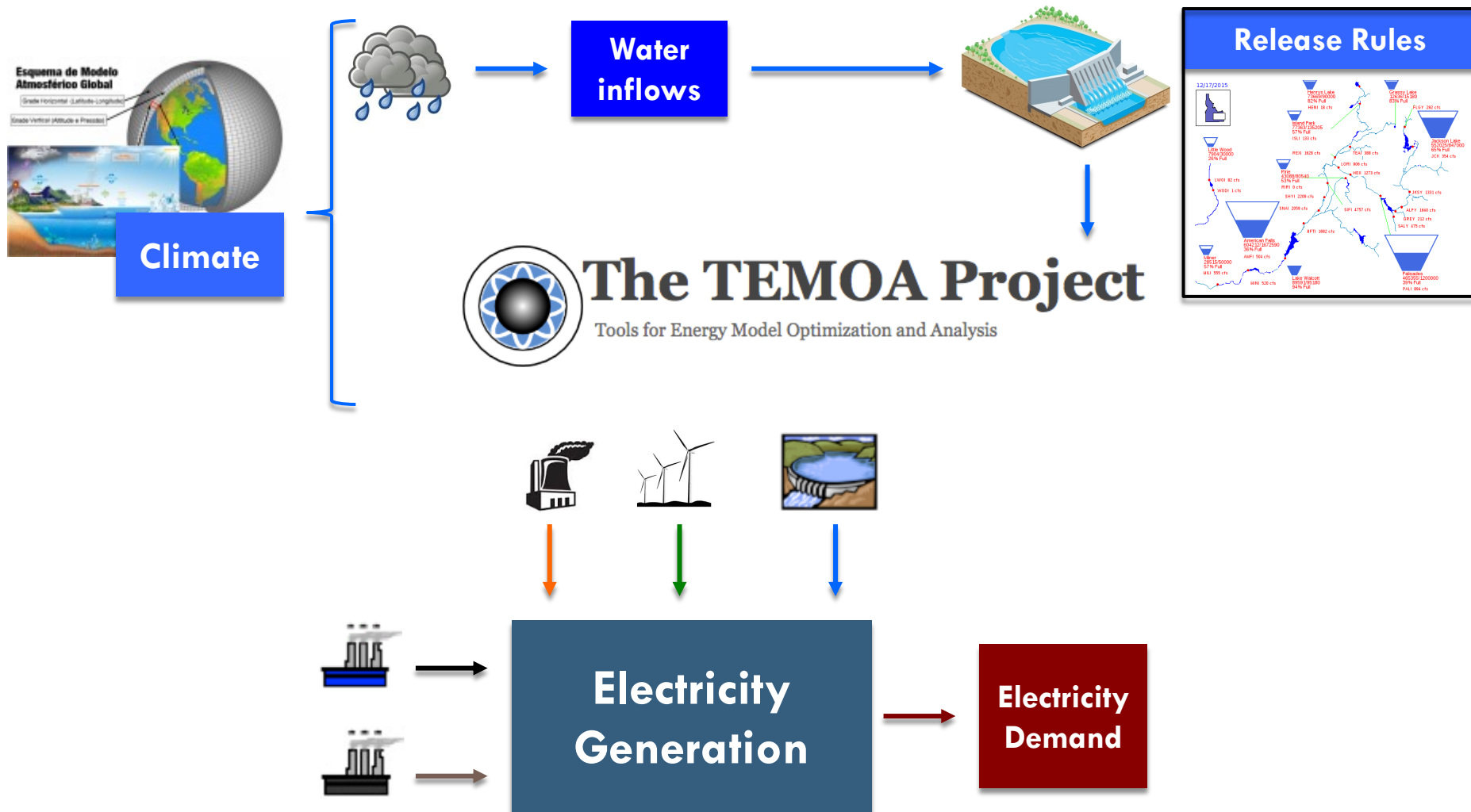
Introduction



- Multiple operational aspects
- Multi-stage problem
- Underlying uncertainties
- Complex decision process



Introduction




Tools for Energy Model Optimization and Assessment

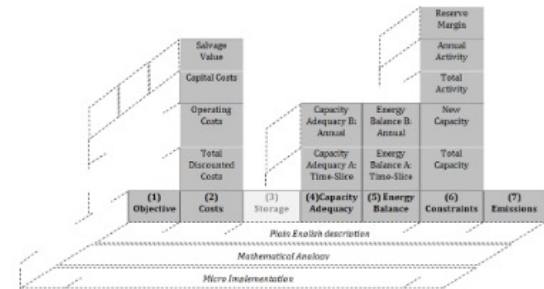
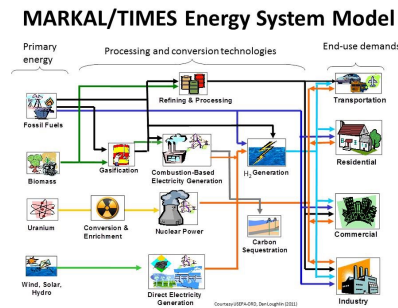
Capacity Expansion Models – Energy Systems

Models for conducting energy system analysis:

- ▣ Markal/Times
- ▣ OSeMOSYS
- ▣ Message

▣ TEMOA

- ▣ Energy economy optimization model
- ▣ Technology assessment and policy analysis at \neq scales
- ▣ Model is implemented in a general algebraic formulation combined with 
- ▣ Stochastic Programming capabilities (extensive LP and Progressive Hedging)



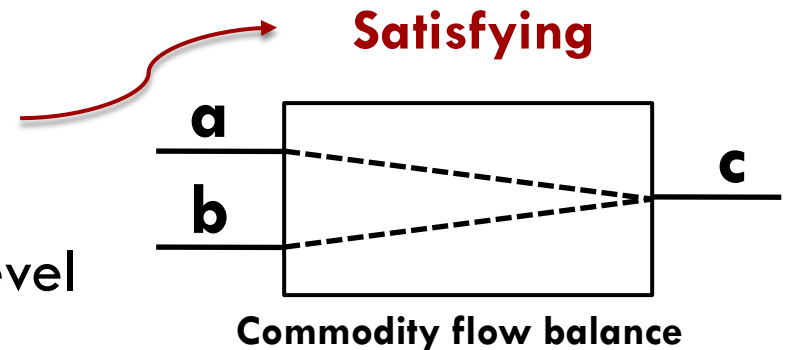
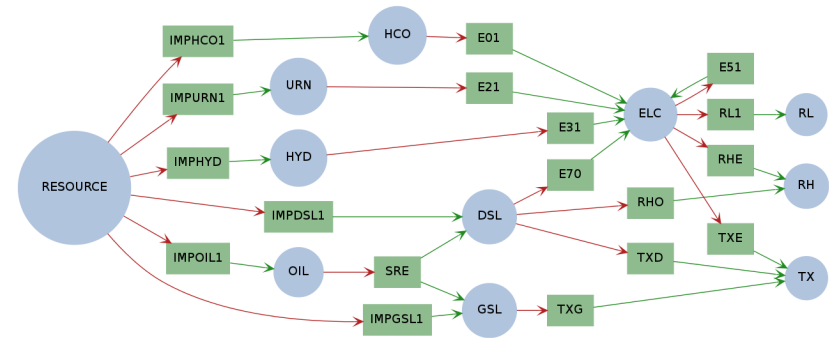
<http://www.temoaproject.org>



TEMOA – General Purpose



- TEMOA represents a capacity expansion and operational model for energy systems
- Represents a multi-stage problem in a network with multiple technologies and multi-commodities
- **Model's objective:** minimize cost of energy supply over a defined time horizon (present + expected future cost)
- Processes represented in a macro level



TEMOA Mathematical Formulation

$$\text{LoanCost} = \sum_{t,v} \left(\left[IC_{t,v} \cdot LA_{t,v} \cdot \sum_{y=0}^{ML_{t,v}} \frac{1}{(1+GDR)^{y+v-P_0}} \right] \cdot \text{CAP}_{t,v} \right)$$

$$\text{FixedCost} = \sum_{p,t,v} \left(\left[FC_{p,t,v} \cdot \sum_{y=0}^{MTL_{p,t,v}} \frac{1}{(1+GDR)^{y+p-P_0}} \right] \cdot \text{CAP}_{t,v} \right)$$

$$\text{VariableCost} = \sum_{p,s,d,t,v} \left(\left[VC_{p,t,v} \cdot \sum_{y=0}^{LEN_p} \frac{1}{(1+GDR)^{y+p-P_0}} \right] \cdot \text{ACT}_{p,s,d,t,v} \right)$$

min **Total Cost = LoanCost + FixedCost + VariableCost**
 ACT,FI,FO
 CAP,CAPVAL

s.t. $\text{ACT}_{p,s,d,t,v} = \sum_{i,o} \text{FO}_{p,s,d,i,t,v,o} \quad \forall \{p,s,d,t,v\} \in \Theta_{\text{activity}}$ **Process activity**

$(CF_{s,d,t,v} \cdot C2A_t \cdot SEG_{s,d} \cdot TLF_{p,t,v}) \cdot \text{CAP}_{t,v} \geq \text{ACT}_{p,s,d,t,v} \quad \forall \{p,s,d,t,v\} \in \Theta_{\text{activity}}$ **Technology capacity**

$\sum_{i,t,v} \text{FO}_{p,s,d,i,t,v,c} \geq DEM_{p,c} \cdot DSD_{s,d,c} \quad \forall \{p,s,d,c \in C^d\} \in \Theta_{\text{demand}}$ **Supply-demand**

$\text{FO}_{p,s,d,i,t,v,o} \leq EFF_{i,t,v,o} \cdot \text{FI}_{p,s,d,i,t,v,o} \quad \forall \{p,s,d,i,t \in T-T^s, v,o\} \in \Theta_{\text{flow}}$ **Process-level commodity flow**

$\sum_{i,t,v} \text{FO}_{p,s,d,i,t,v,c} \geq \sum_{t,v,o} \text{FI}_{p,s,d,c,t,v,o} \quad \forall \{p,s,d,c\} \in \Theta_{\text{balance}}$ **Global commodity balance**

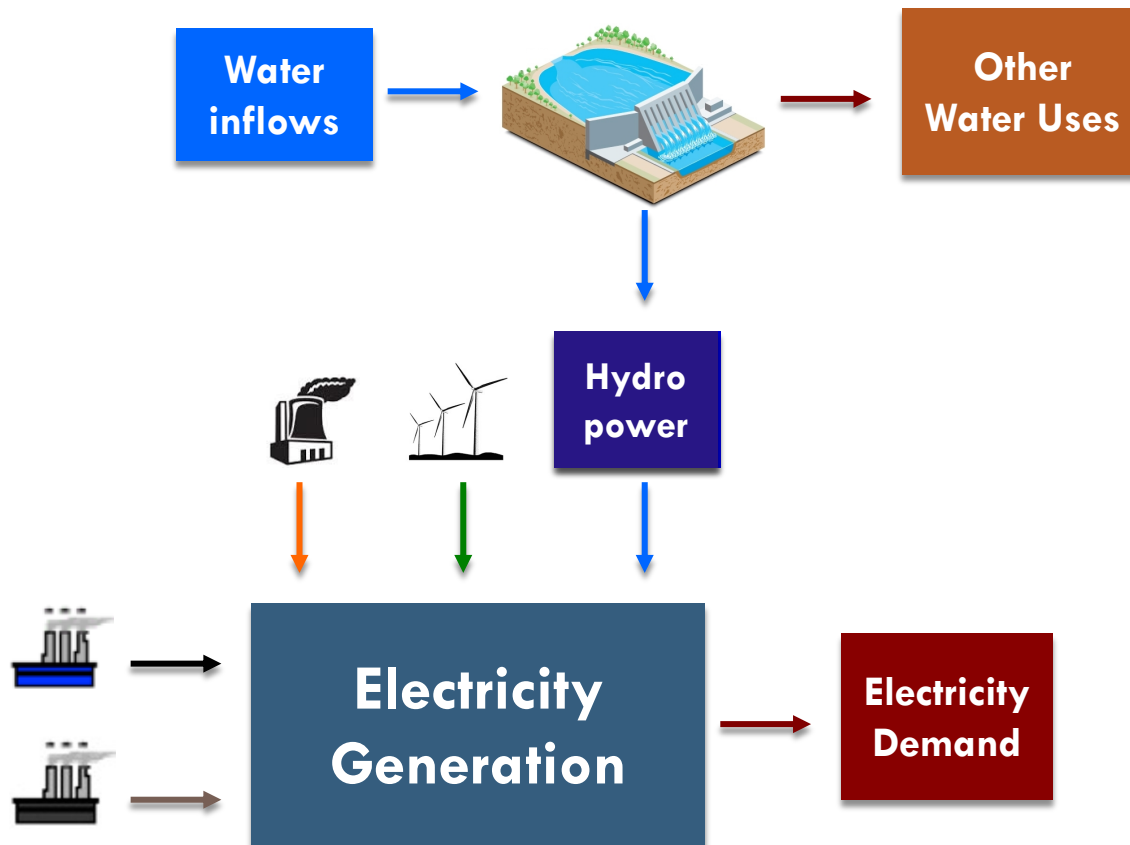
Other constraints and bounds: baseload, emissions, battery storage,...

From Capacity Expansion to Power Generation Scheduling

Modeling Goals

- Represent a short-term problem with monthly discretization for time periods
- Improve the representation of the system dynamics
- Include randomness in terms of resource availability at each time period

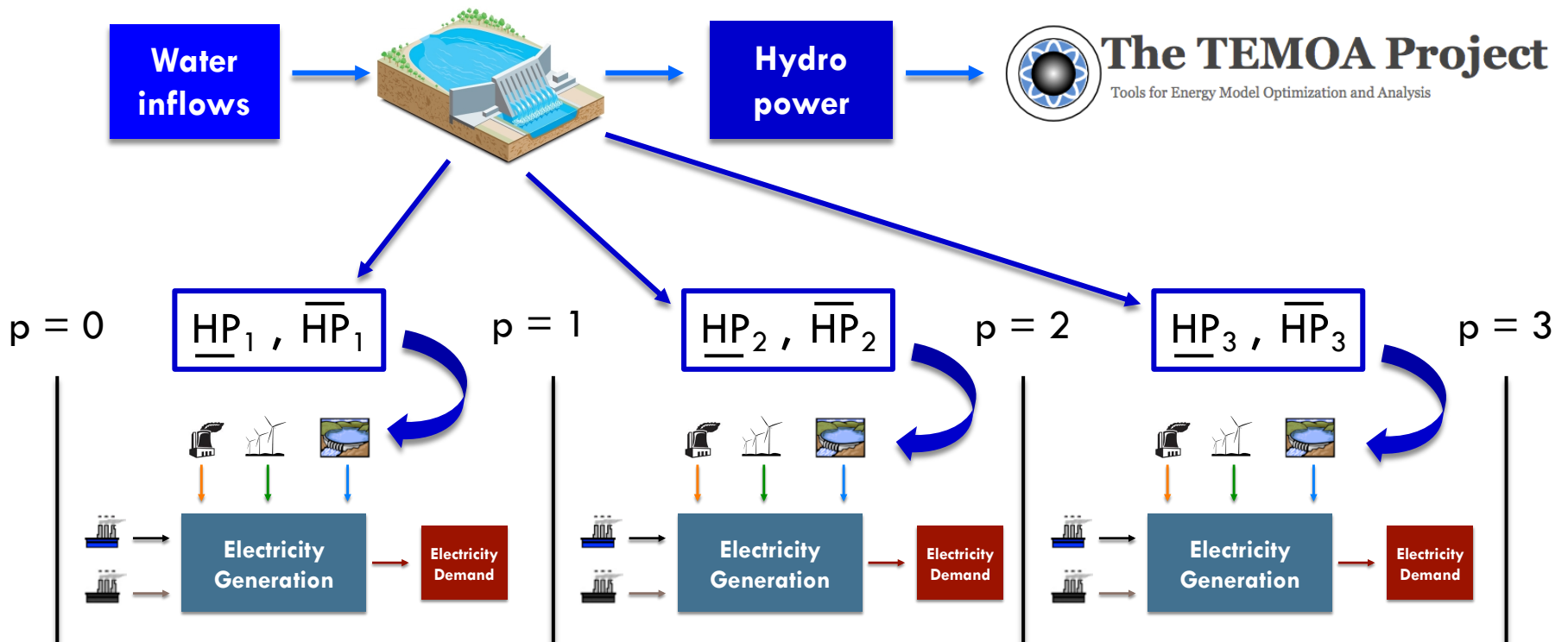
Modeling Goals (cont.)



Notation and Previous Model

□ A little about notation:

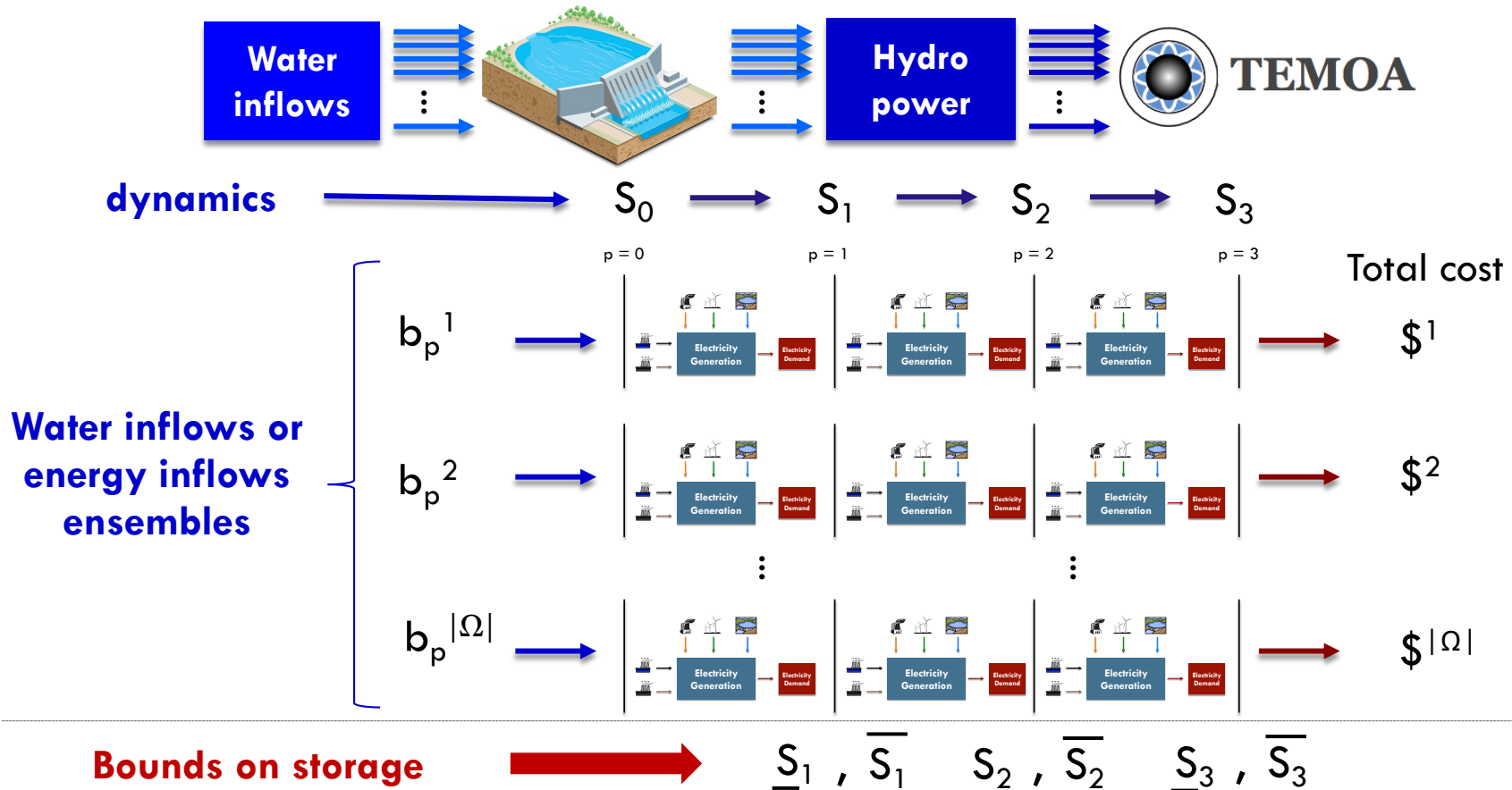
- We will index time periods by p
- \underline{HP} and \overline{HP} represents minimum and maximum bounds for hydro power in [aMW]
- S_p storage values at time period p and \underline{S} and \overline{S} are min and max bounds on storage [hm^3]
- b_p^1 represents the water inflows in [hm^3] over the course of time period p at hydro plant 1



Enhancing TEMOA Formulation

□ Let's talk about a stochastic representation

□ For each scenario $\omega \in \Omega$, the forecasting model model should provide: b_p^ω



Enhancing TEMOA Formulation (cont.)

- Model needs to carry out information from one month to the other

- A new decision vector is needed:

S_p : end of period storage for hydro plants

Water inflows

- New constraints are needed:

(Mass balance constraint) $S_p = S_{p-1} + b_p - \sum FO_p$

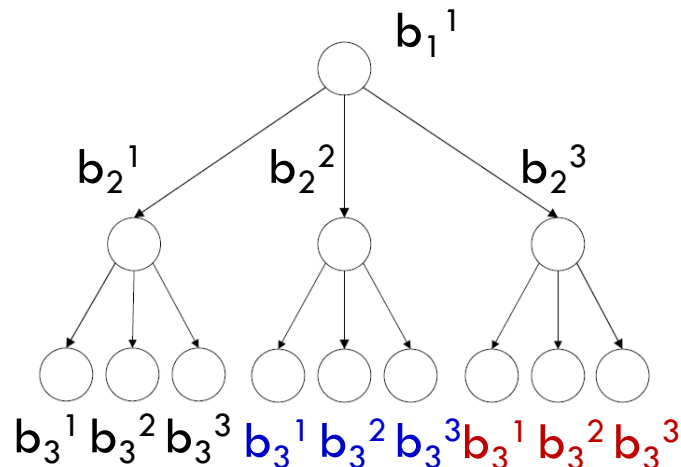
(Storage bounds)

$$\underline{S}_p \leq S_p \leq \bar{S}_p$$

Water releases

- By adding that the model has the possibility to make operational recourse actions \longrightarrow **Multi-stage stochastic linear program (SLP-p)**

Scenario tree



General TEMOA Model

min ACT, FI, FO	Total Cost = FixedCost + VariableCost		
s.t.	$ACT_{p,s,d,t,v} = \sum_{i,o} FO_{p,s,d,i,t,v,o} \quad \forall \{p,s,d,t,v\} \in \Theta_{\text{activity}}$		Process activity
	$(CF_{s,d,t,v} \cdot C2A_t \cdot SEG_{s,d} \cdot TLF_{p,t,v}) \cdot CAP_{t,v} \geq ACT_{p,s,d,t,v} \quad \forall \{p,s,d,t,v\} \in \Theta_{\text{activity}}$		Technology capacity
	$\sum_{i,t,v} FO_{p,s,d,i,t,v,c} \geq DEM_{p,c} \cdot DSD_{s,d,c} \quad \forall \{p,s,d,c \in C^d\} \in \Theta_{\text{demand}}$		Supply-demand
	$FO_{p,s,d,i,t,v,o} \leq EFF_{i,t,v,o} \cdot FI_{p,s,d,i,t,v,o} \quad \forall \{p,s,d,i,t \in T - T^s, v,o\} \in \Theta_{\text{flow}}$		Process-level commodity flow
	$\sum_{i,t,v} FO_{p,s,d,i,t,v,c} \geq \sum_{t,v,o} FI_{p,s,d,c,t,v,o} \quad \forall \{p,s,d,c\} \in \Theta_{\text{balance}}$		Global commodity balance
	$S_p = S_{p-1} + \tilde{b}_p - \sum FO_p$	$\underline{S}_p \leq S_p \leq \bar{S}_p$	Water balance and bounds
Random water inflows	Other constraints and bounds,...		

Power Generation Scheduling as SLP-p

A general model for power generation scheduling would be



$$\begin{aligned} \min_{x_1} \quad & c_1 x_1 + E_{b_2|b_1} h_2(x_1, b_2) \\ \text{s. t.} \quad & A_1 x_1 = B_1 x_0 + b_1 \\ & x_1 \geq 0 \end{aligned}$$

where, for $p = 2, \dots, P$



$$\begin{aligned} \min_{x_p} \quad & c_p x_p + E_{b_{p+1}|b_1, \dots, b_p} h_{p+1}(x_p, b_{p+1}) \\ \text{s. t.} \quad & A_p x_p = B_p x_{p-1} + b_p \\ & x_p \geq 0 \end{aligned}$$

x_p : stage p decision variables including: technologies activity (hydro generation, thermal generation), resources activity, water storage at reservoirs

c_p : cost vector related to technology and resource usage

A_p : constraint matrix including supply-demand, process-level commodity flow, global commodity water balance, ...

b_p : stochastic water inflow at each hydro plant and deterministic demand

$B_p x_{p-1}$: storage from last stage

Case Study

Deterministic Case Study

TEMOA Input Parameters Specs

- We are interested in problems for short horizons
- Time horizon: 3 months $\rightarrow P^f = \{1,2,3,4\}$
- Seasons: 4 weeks $\rightarrow S = \{W_1, W_2, W_3, W_4\}$
- Time of the day: 3 slices $\rightarrow D = \{\text{day, night, peak}\}$
- Discount rate 1% per month $\rightarrow GDR = 0.01$
- Capacity-activity conversion factor 31.536 (year) \rightarrow 2.628 (month)

HydroStorage Case Study – Instances

□ Case Hydro:

- $DEM_{1c} = 110$ [PJ] $DEM_{2c} = 130$ [PJ] $DEM_{3c} = 150$ [PJ]
- **Coal thermal plant** $MAX_1 = 36$ [GW] **Wind Farm** $MAX_2 = 100$ [GW]
- **Hydropower** installed capacity = **20**[GW]
- **Efficiency: Hydro** → **ELC = 0.9**

□ Case HydroStorage:

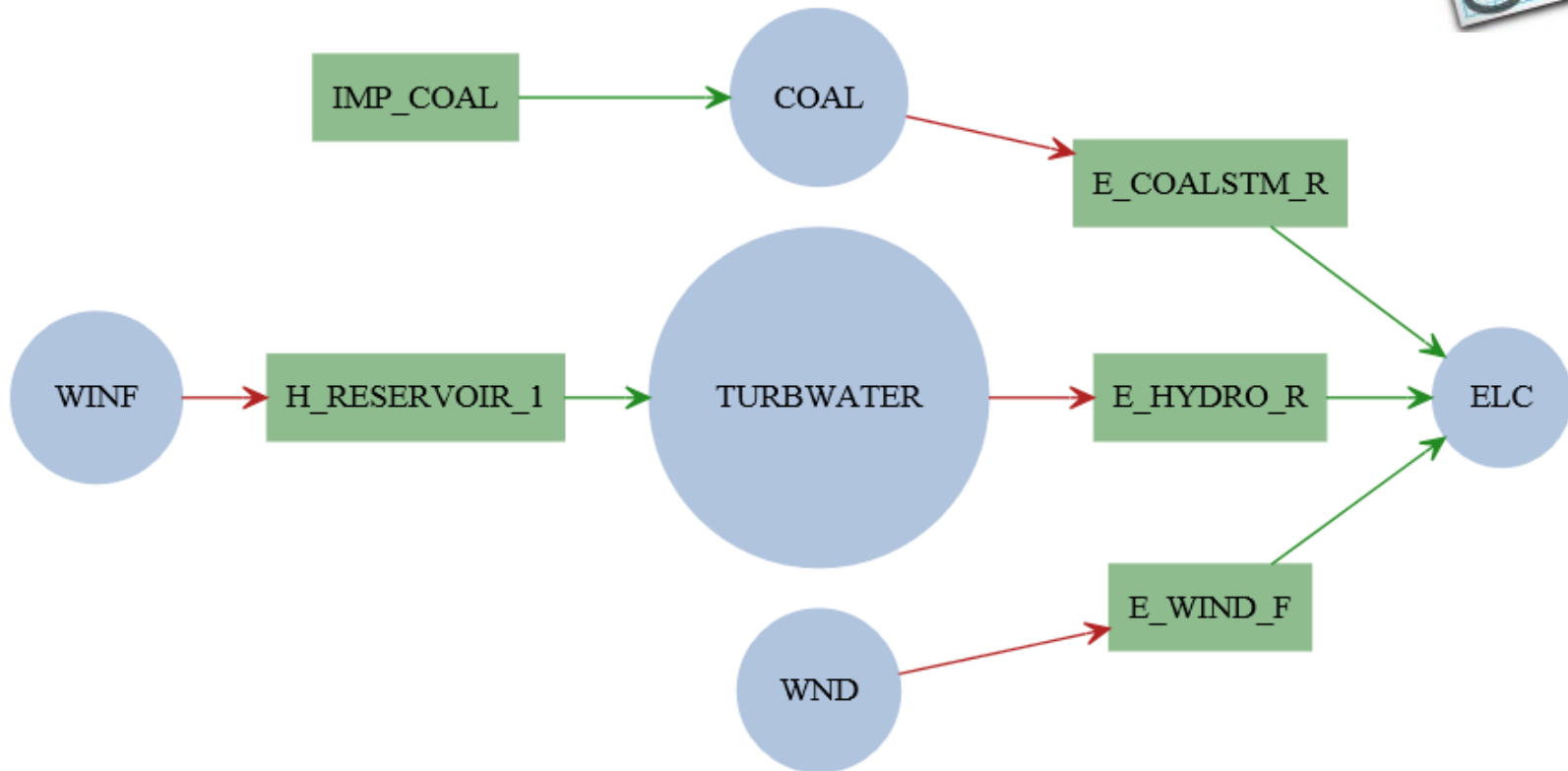
- **Hydropower** installed capacity = **20**[GW]
- **Initial Storage = 10** **Water Inflows** = [10, 10, 50]
- **Efficiency: Reservoir** → **TurbWater = 1.0**
- **Thermal Cost in** $P^f = 3$ **increased from 3** → **3.5** [M\$/PJ]

□ Case HydroStorage+:

- **Hydropower** installed capacity = **25**[GW]

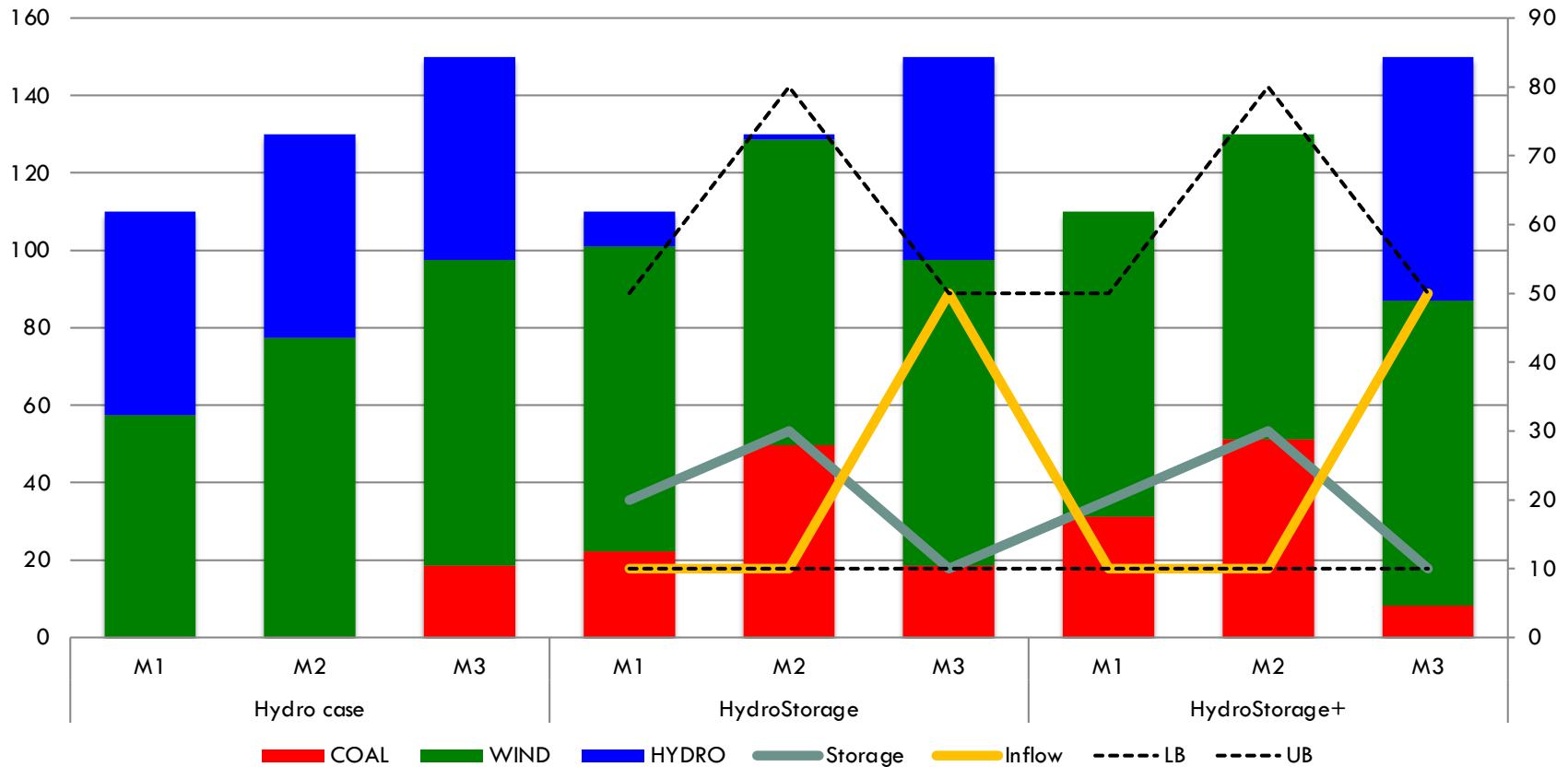
Network Representation

- Python script → graphical representation (Graphviz)



Deterministic Case Study - Results

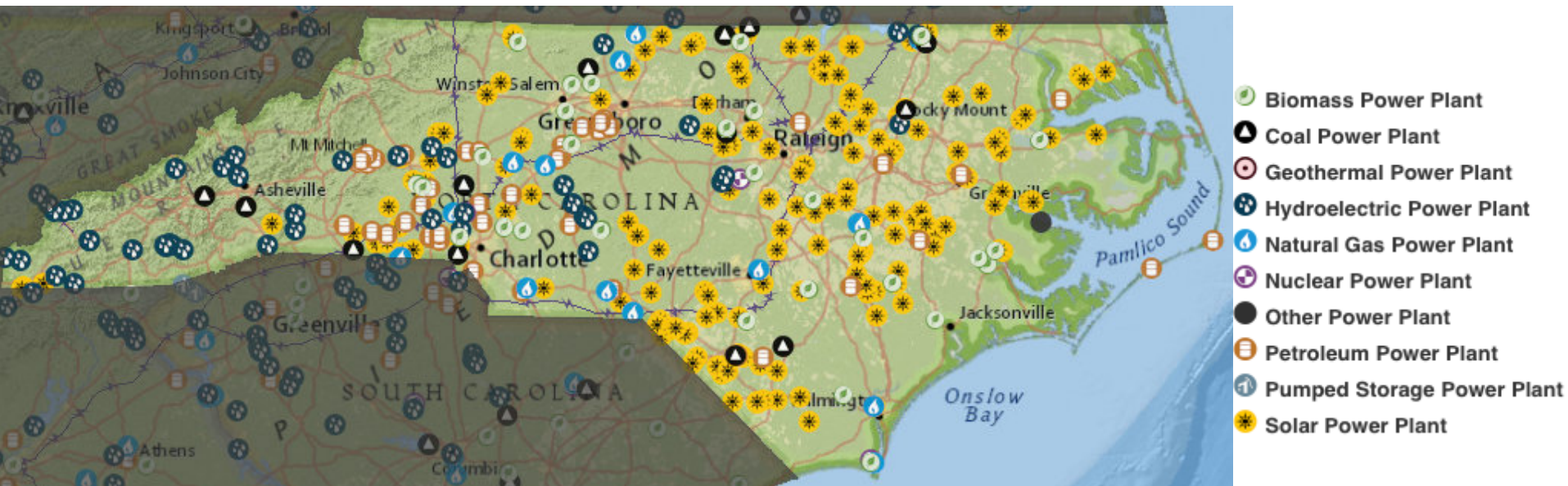
Power Generation Dispatches - Three Techs Case Study



North Carolina Case Study

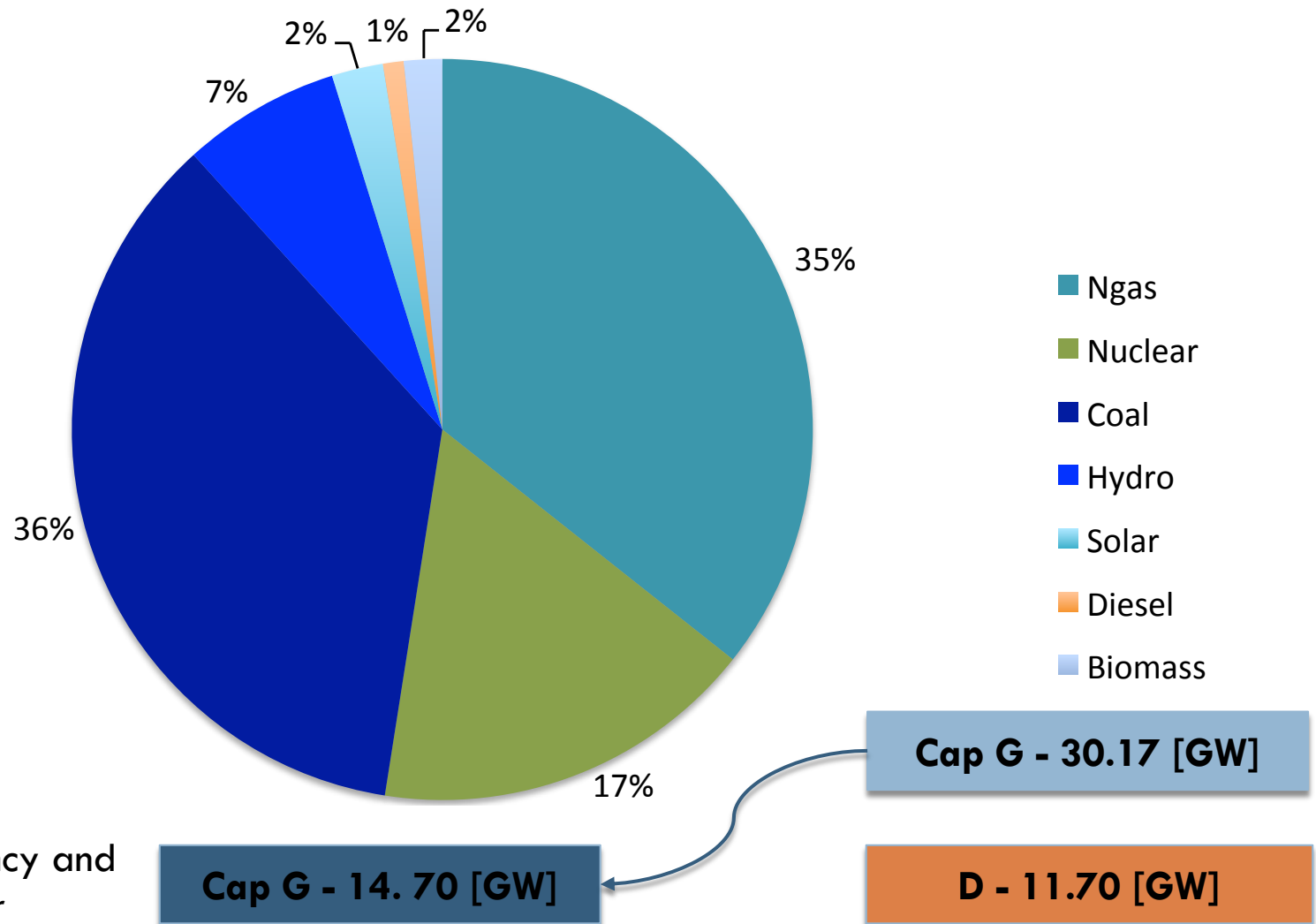
North Carolina State – Case Study

- Input information adapted from EIA database



- We consider only the installed capacity in year 1
- For this case study we aim to solve 4-stage problems

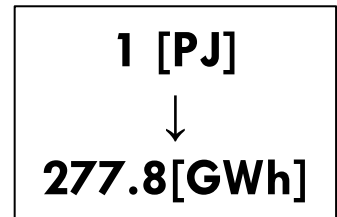
Installed Capacity – NC Case Study



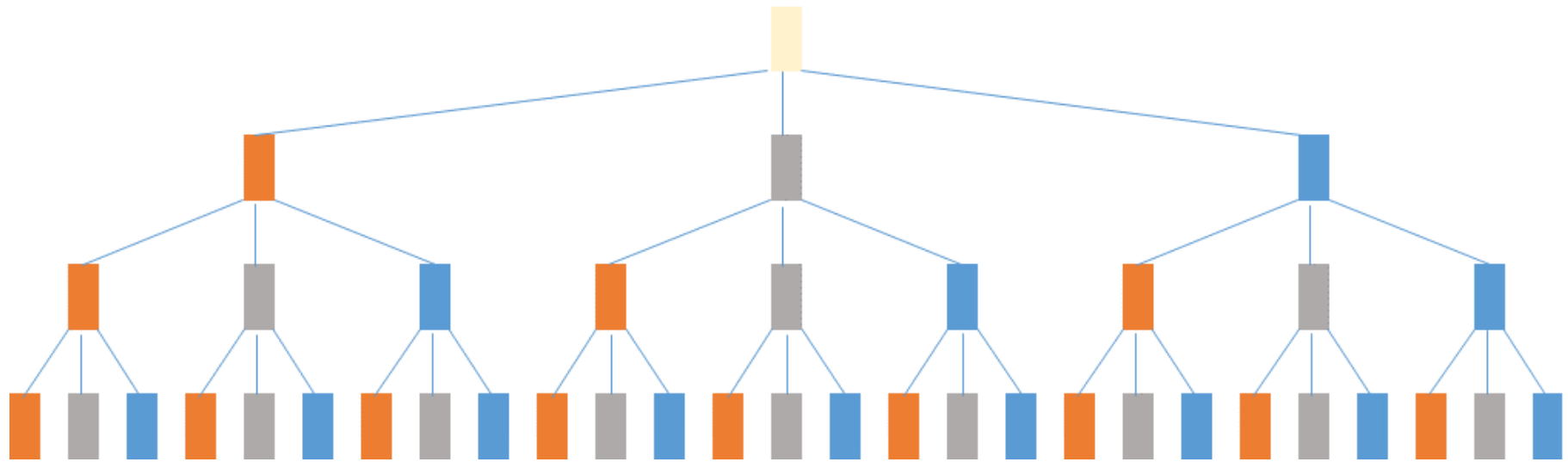
* After efficiency and capacity factor

TEMOA Input Parameters Specs

- Time horizon: 4 months $\rightarrow P^f = \{1,2,3,4,5\}$
- Seasons: 4 weeks $\rightarrow S = \{W_1, W_2, W_3, W_4\}$
- Time of the day: 4 slices $\rightarrow D = \{\text{am, pm, peak, night}\}$
- Discount rate 1% per month $\rightarrow GDR = 0.01$
- Capacity-activity conversion factor 2.628 (month)
- Demand at each stage:
 $DEM_{1c} = 30.75 \text{ [PJ]}, DEM_{2c} = 30.75 \text{ [PJ]}, DEM_{3c} = 30.75 \text{ [PJ]}, DEM_{4c} = 30.75 \text{ [PJ]}$
- Base case:
 - **Coal** $MAX_1 = 10.8 \text{ [GW]}$, **NGas** $MAX_2 = 10.7 \text{ [GW]}$, **Nuclear** $MAX_3 = 5.1 \text{ [GW]}$
 - **Hydropower** installed capacity +/- **2 [GW]** & **Other = 1.5 [GW]**
- **Other cases:** $DEM_{1c} = 15.375 \text{ [PJ]}$ / $DEM_{1c} = 4.3 \text{ [PJ]}$ / Reduced water inflows at scenario low



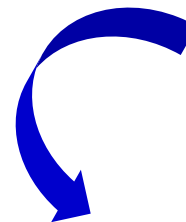
Scenario Tree for NC Instance



**Probabilities
estimated using
EIA monthly
generation data
since 2000**

	M_H/A_H	0.25	J_H/M_H	0.75	
	M_A/A_H	0.625	J_A/M_H	0.2	
	M_L/A_H	0.125	J_L/M_H	0.05	
A_H/M_A	0.2	M_H/A_A	0.25	J_H/M_A	0.08
A_A/M_A	0.70	M_A/A_A	0.58	J_A/M_A	0.58
A_L/M_A	0.10	M_L/A_A	0.17	J_L/M_A	0.34
	M_H/A_L	0.1	J_H/M_L	0.06	
	M_A/A_L	0.5	J_A/M_L	0.56	
	M_L/A_L	0.4	J_L/M_L	0.38	

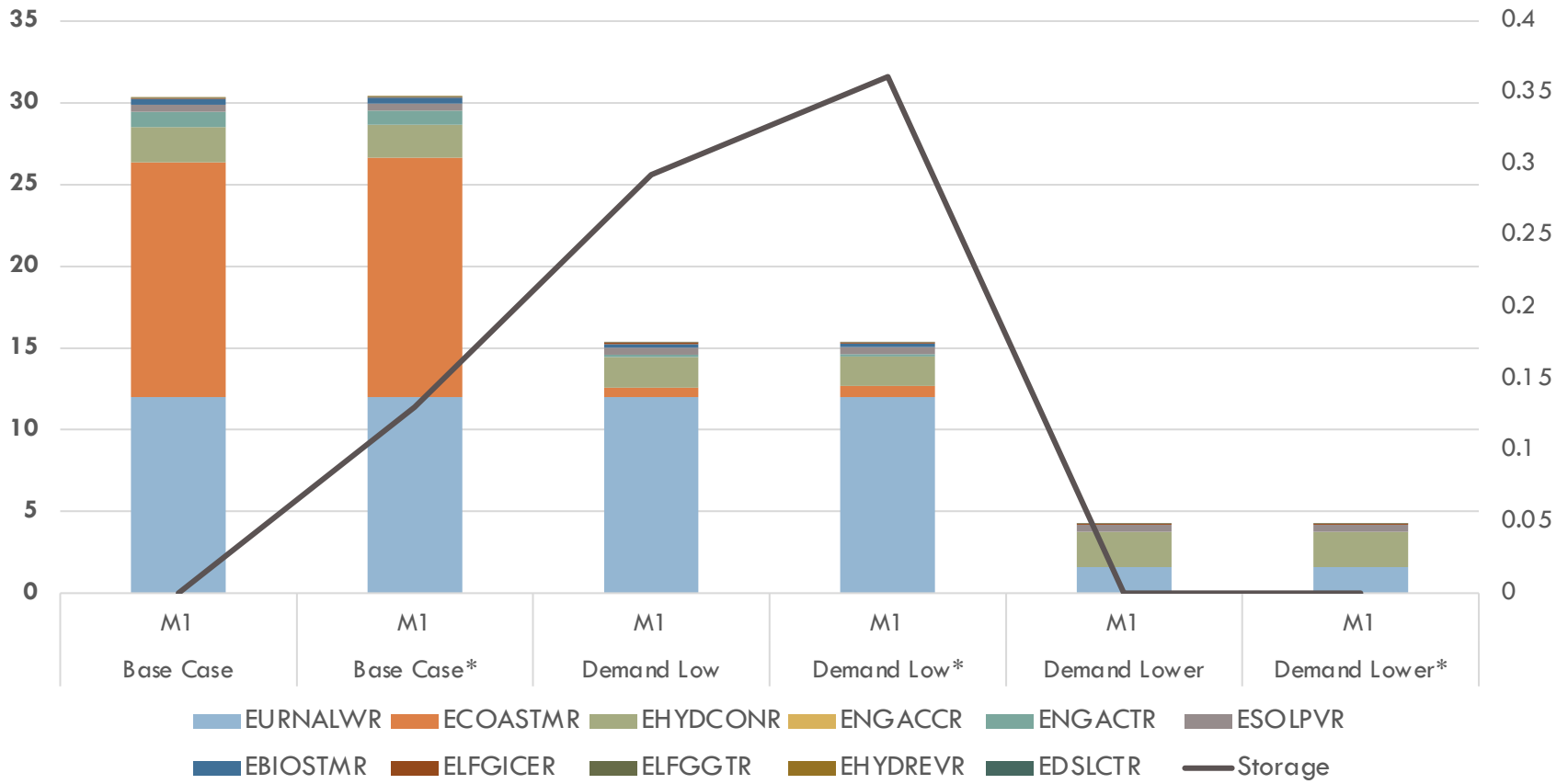
**Artificial water
inflows produced
from generation data
[10³hm³-month]
(2.78 → 820.71 [aMW])**



	March	April	May	June
		3.30	3.13	3.65
2.78		2.44	2.04	2.13
		1.92	1.70	1.74

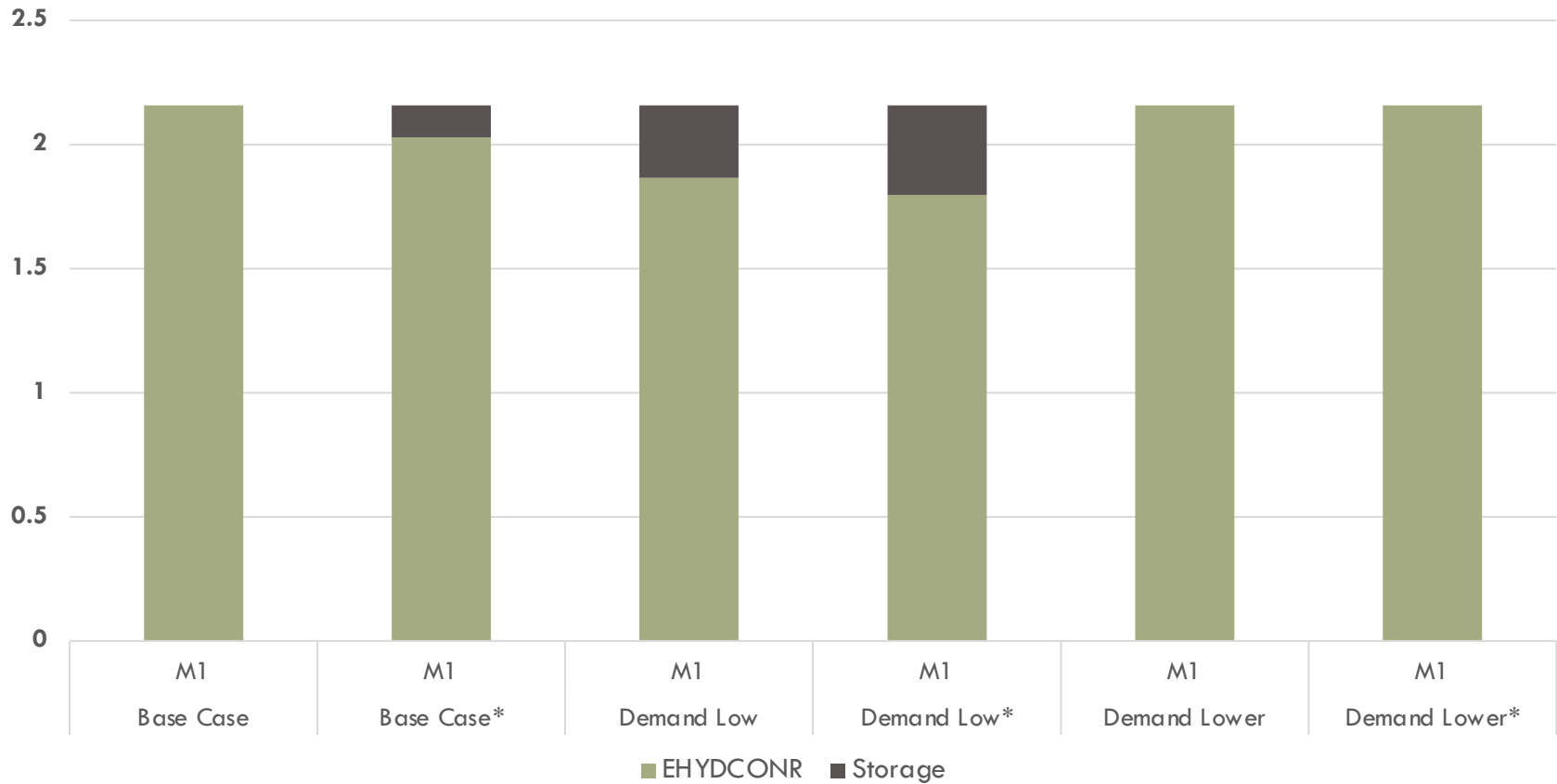
North Carolina Case Study – Results (cont.)

Power Generation Dispatches and Storage [PJ] - NC Case Study



North Carolina Case Study – Results (cont.)

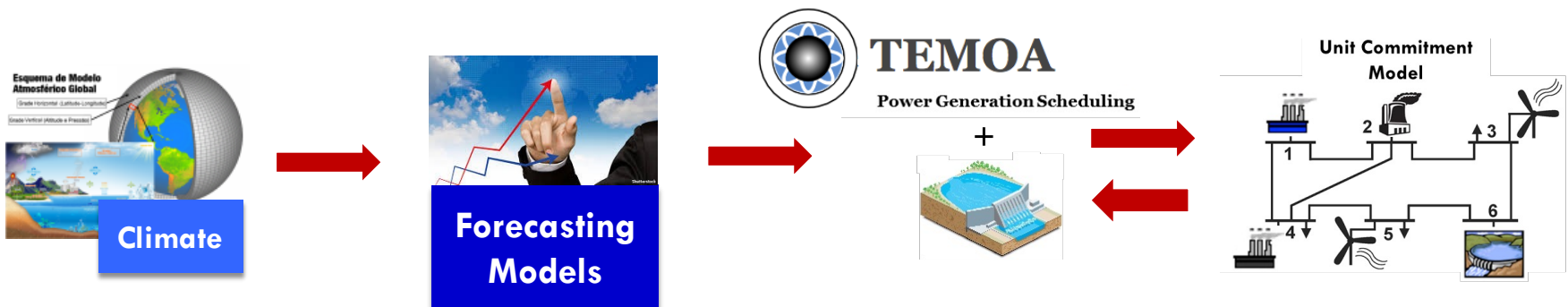
Hydro Generation Dispatch and Storage [PJ] - NC Case Study



Nexts Steps & Final Comments

Next Steps & Final Comments

- Define a balanced study case in terms of a hydro and thermal generation in a system with reservoir storage
- Formulation of a combined framework in a closed-loop form to solve scheduling problem and & unit commitment
- Add climate information to resource supply availability and electricity demand → generate future scenarios
- Represent large-size problems and provide a solution methodology using Sampling-based Decomposition Algorithms



References

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THANK YOU !

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